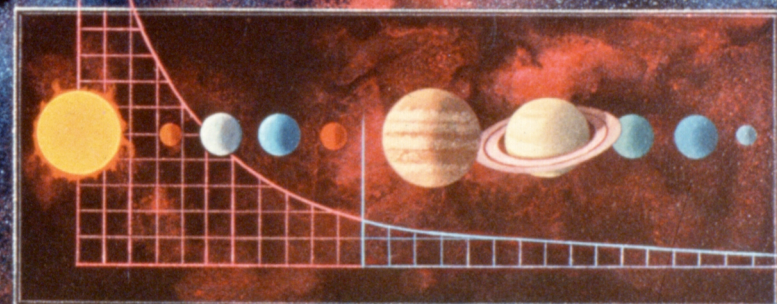
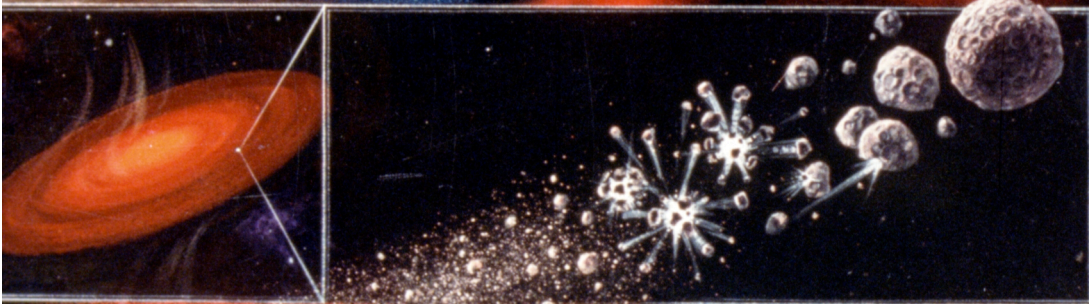
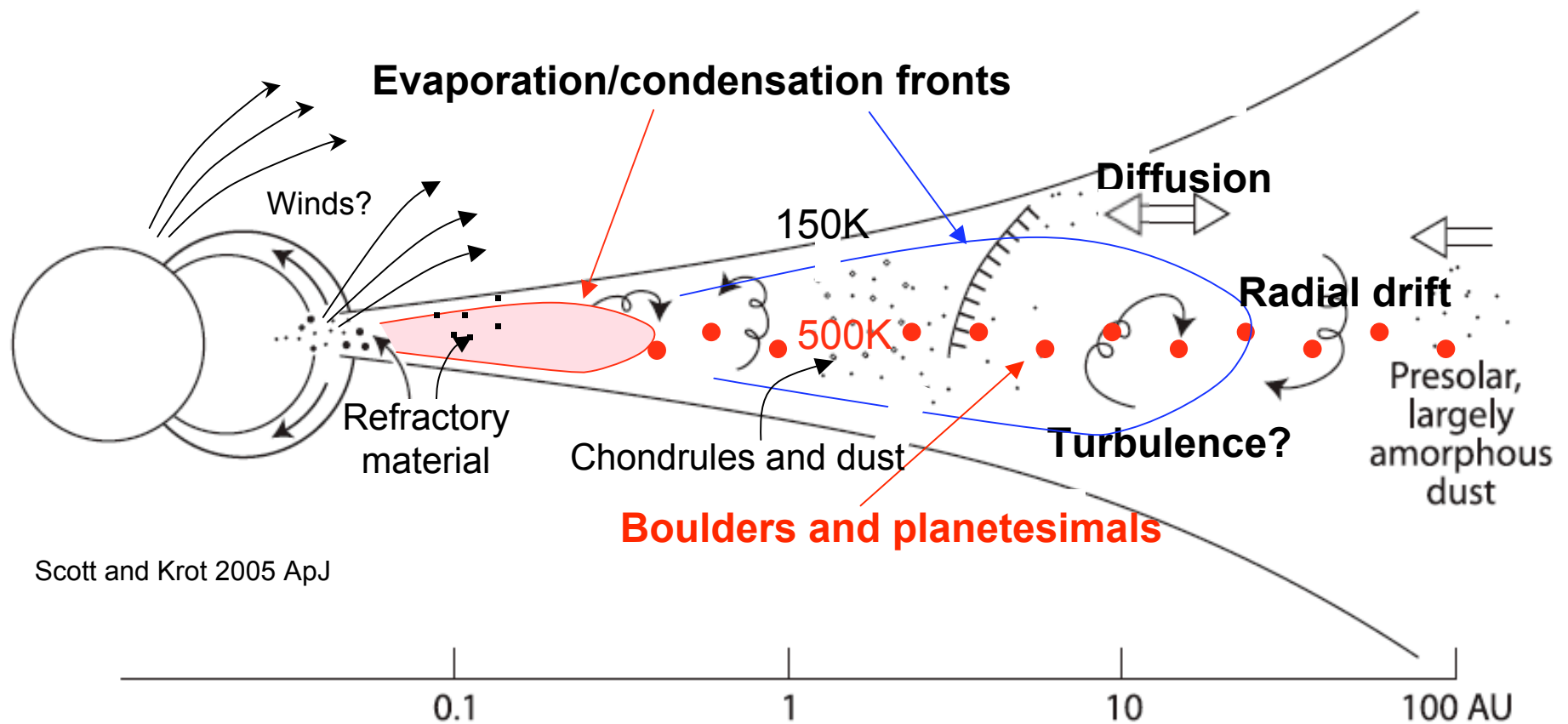
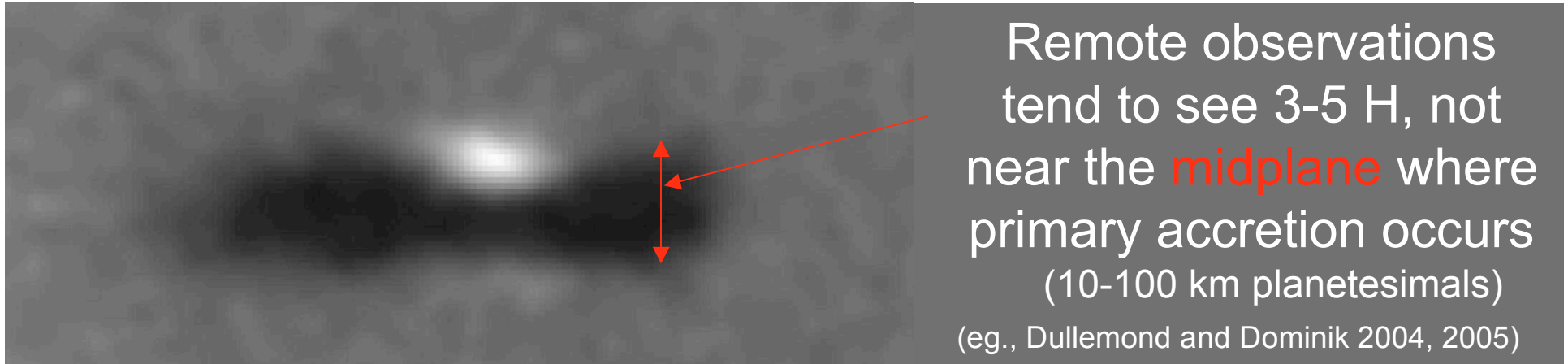




# Evolution of solids in the protoplanetary nebula and Primary accretion of planetesimals



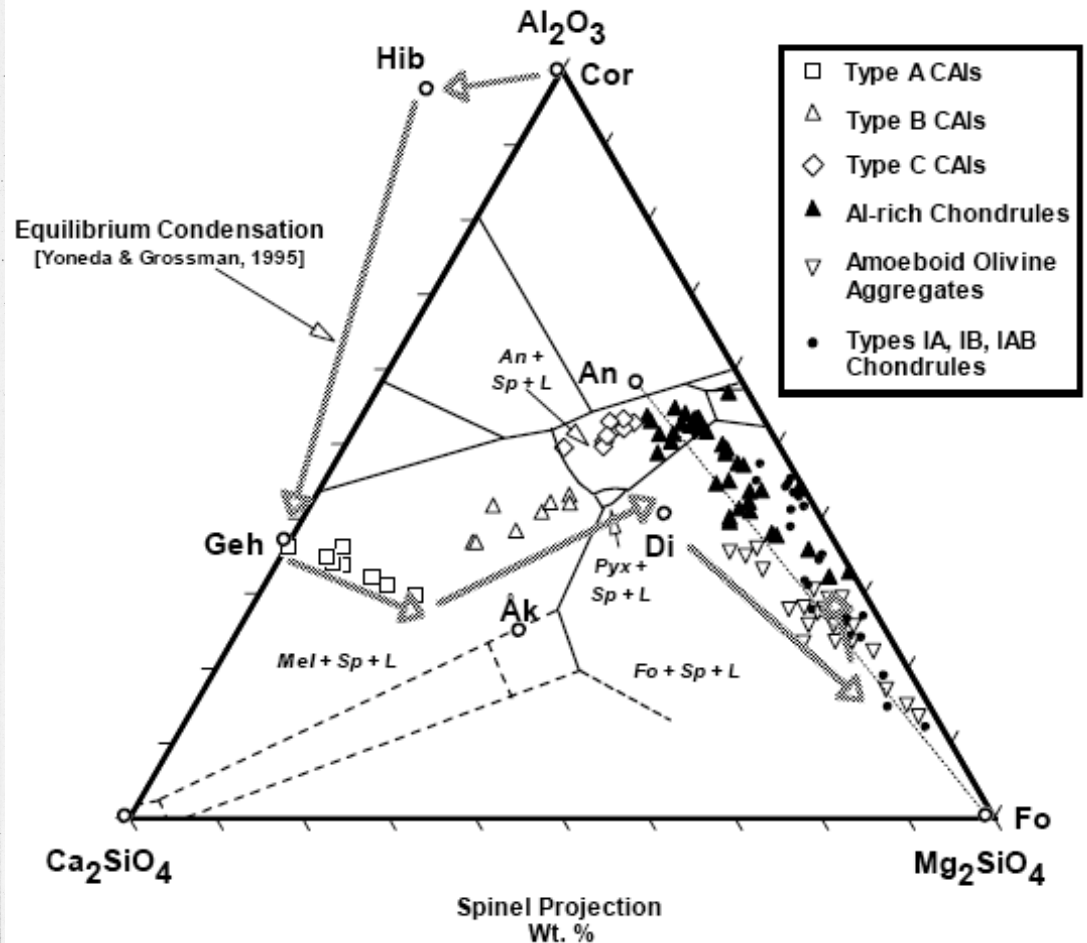




Scott and Krot 2005 ApJ

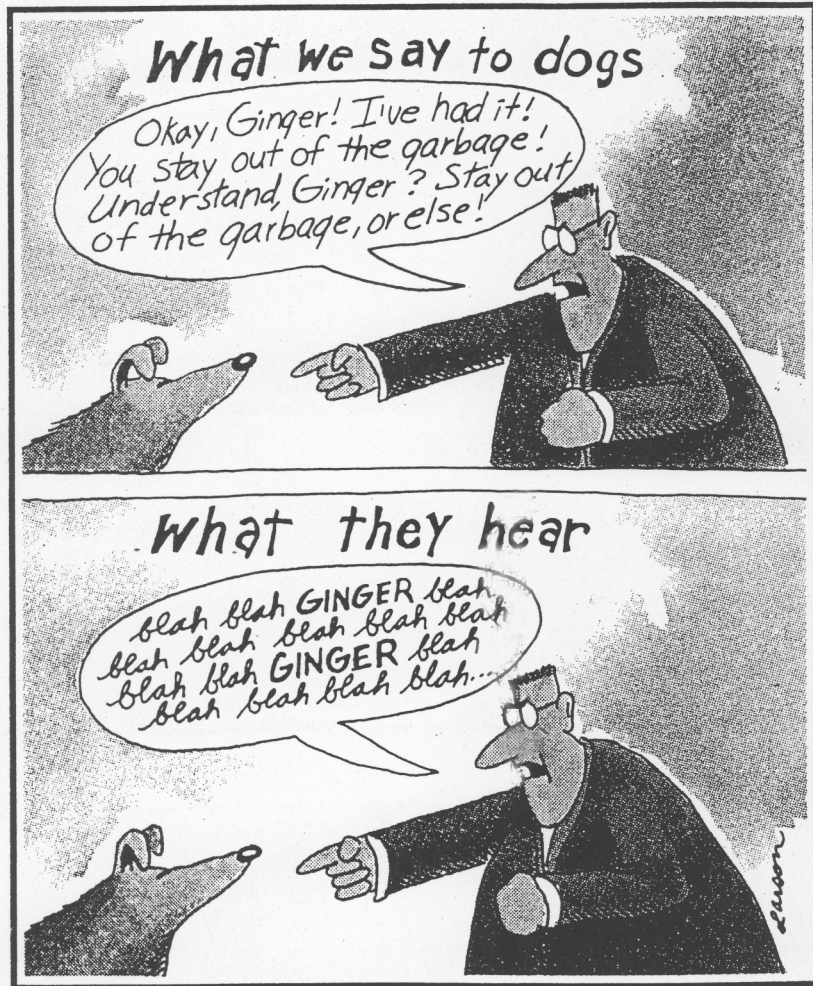


# Communication between meteoriticists and astrophysicists is a serious problem





# Communication between meteoriticists and astrophysicists is a serious problem



$$\begin{aligned} \bar{\rho}_p \frac{\partial}{\partial t} \bar{u}_p + \bar{\rho}_p \bar{w}_p \frac{\partial}{\partial z} \bar{u}_p &= 2(\bar{\rho}_p v_p^* + \overline{\rho_p' v_p'}) v_K / r \\ &- \frac{\partial}{\partial z} (\bar{\rho}_p \overline{u_p' w_p'}) - \frac{\partial}{\partial z} (\overline{\rho_p' u_p' w_p}) - \overline{\rho_p' w_p'} \frac{\partial}{\partial z} \bar{u}_p \\ &- \bar{\rho}_p (\bar{u}_p - \bar{u}_g) / t_s, \quad (9) \end{aligned}$$

$$\begin{aligned} \bar{\rho}_p \frac{\partial}{\partial t} v_p^* + \bar{\rho}_p \bar{w}_p \frac{\partial}{\partial z} v_p^* &= -\frac{1}{2}(\bar{\rho}_p \bar{u}_p + \overline{\rho_p' u_p'}) v_K / r \\ &- \frac{\partial}{\partial z} (\bar{\rho}_p \overline{v_p' w_p'}) - \frac{\partial}{\partial z} (\overline{\rho_p' v_p' w_p}) - \overline{\rho_p' w_p'} \frac{\partial}{\partial z} v_p^* \\ &- \bar{\rho}_p (\eta v_K + v_p^* - v_g^*) / t_s, \quad (10) \end{aligned}$$

$$\begin{aligned} \frac{\partial}{\partial t} (\bar{\rho}_p \bar{w}_p) + \frac{\partial}{\partial z} (\bar{\rho}_p \bar{w}_p^2) &= -\bar{\rho}_p G M z / r^3 \\ &- \frac{\partial}{\partial z} (\bar{\rho}_p \overline{w_p' w_p'}) - 2 \frac{\partial}{\partial z} (\overline{\rho_p' w_p' w_p}) - \bar{\rho}_p \bar{w}_p / t_s. \quad (11) \end{aligned}$$



# Overview

Evidence from primitive bodies in our solar system

The importance of turbulence

Particle collisions: sticking or disruption

Radial drift of particles; evaporation fronts

A scenario for primary accretion



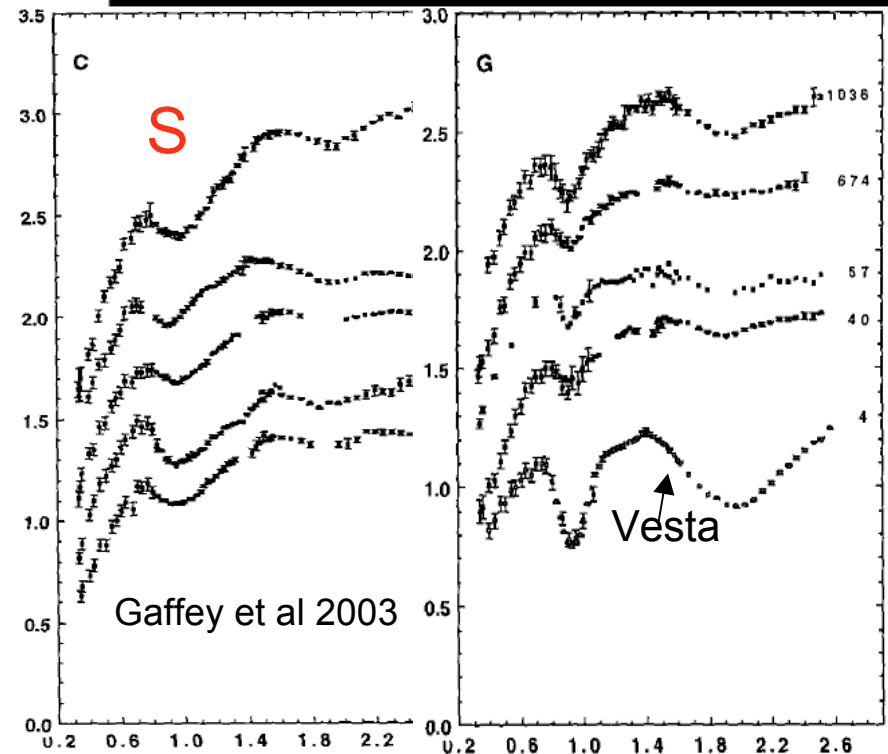
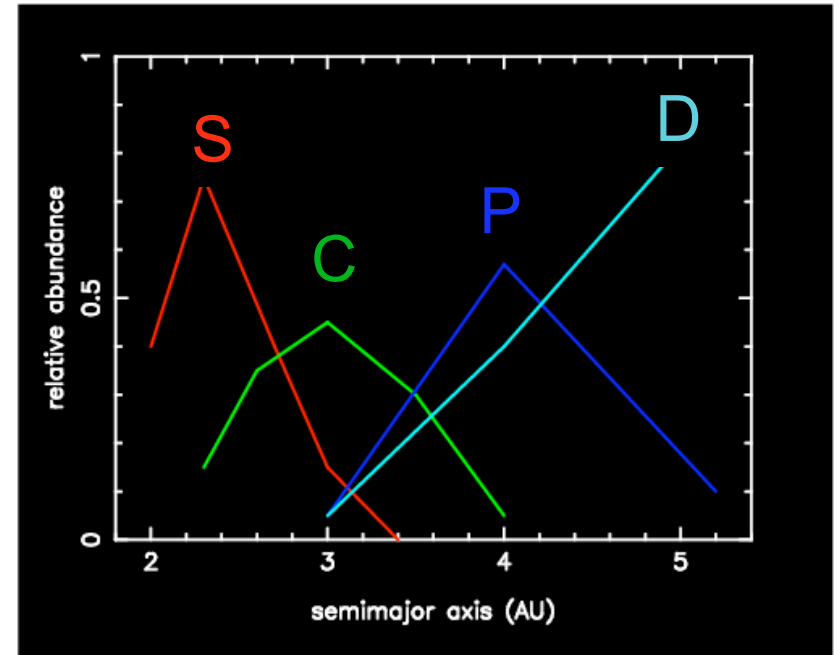
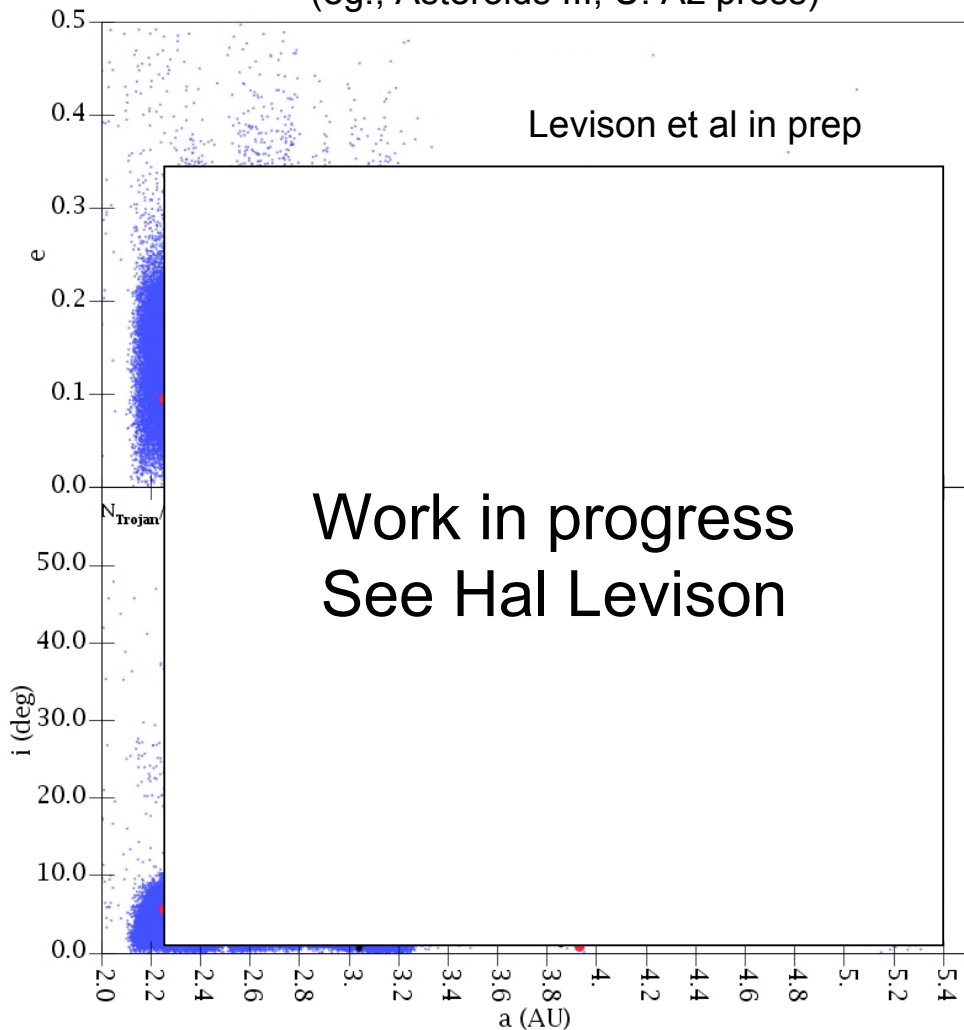
# Asteroids

*Radially zoned;*

*Some members formed elsewhere;*

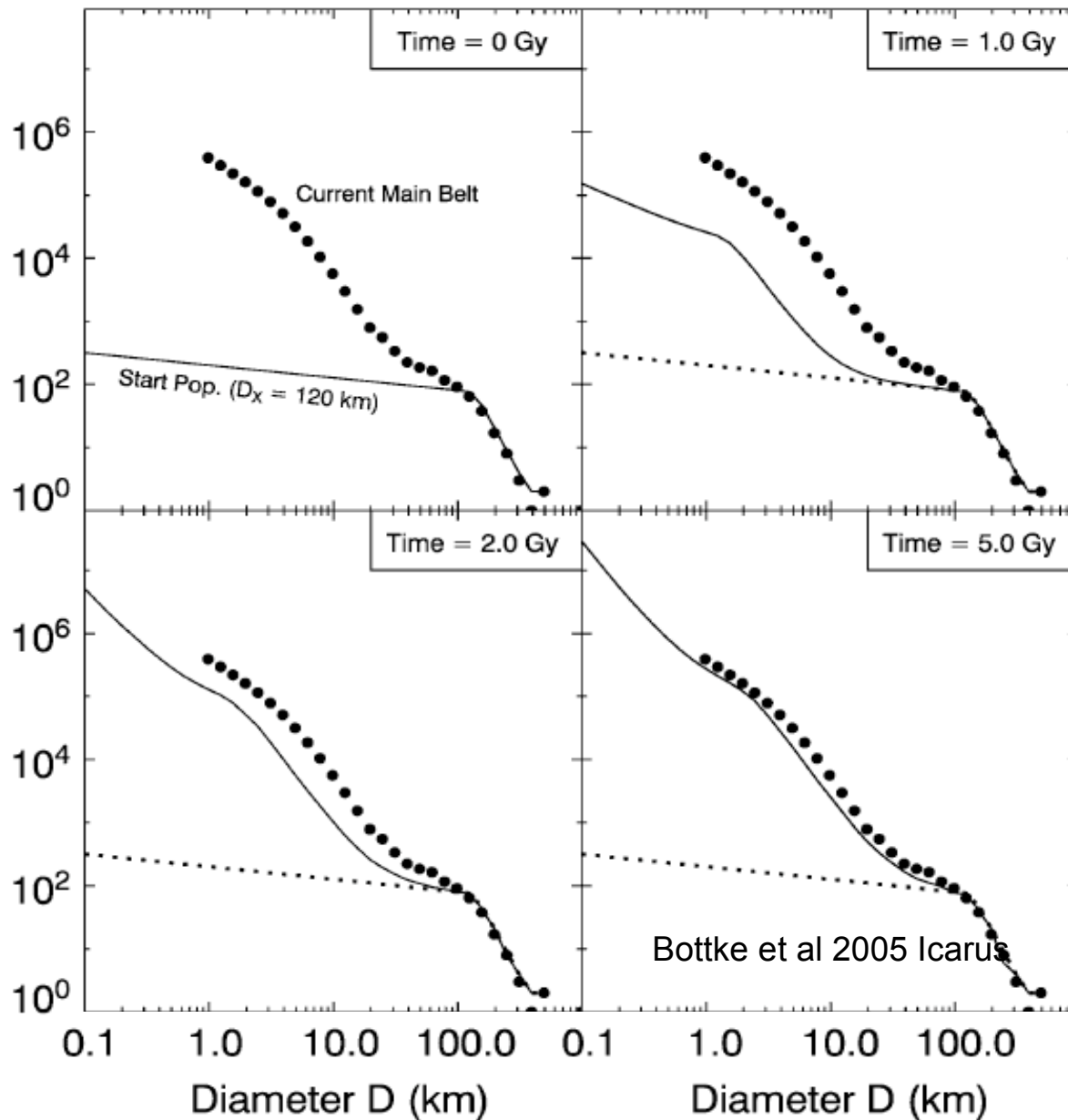
*Few ever melted significantly*

(eg., Asteroids III, U. Az press)





# The violent youth of primitive bodies



**Collisional evolution**  
after nebula gas dispersed  
and Jupiter formed  
was unable to destroy  
primordial 100km objects

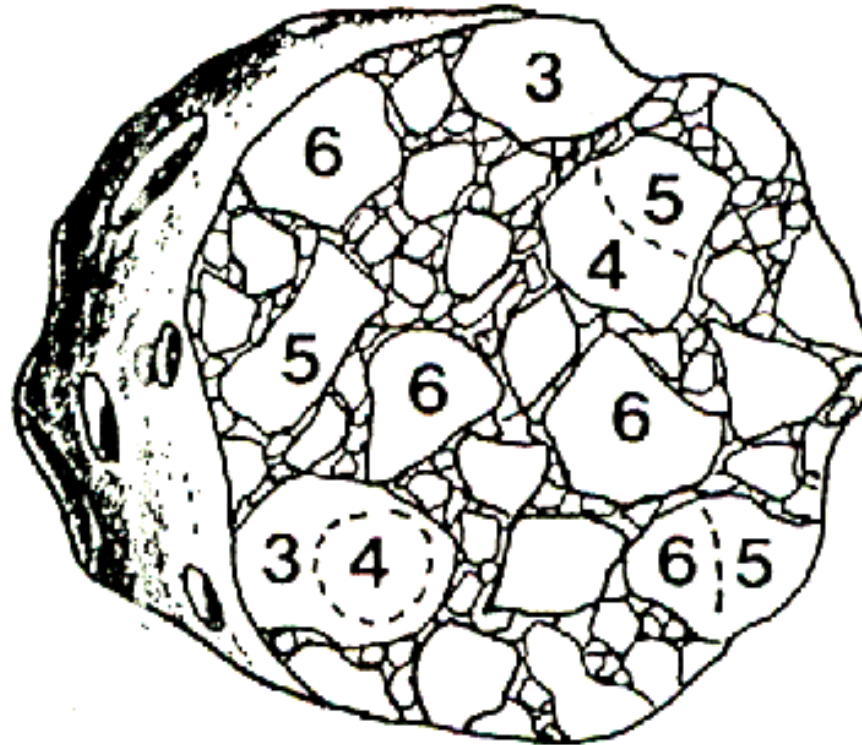
(but nearly everything  
smaller is secondary)

*Most primordial mass  
was in 100-km objects*

D-type asteroids,  
Kuiper Belt Objects  
may have similar  
initial size distributions



**Post-primary-accretion collisional environment left many asteroids as rubble piles**

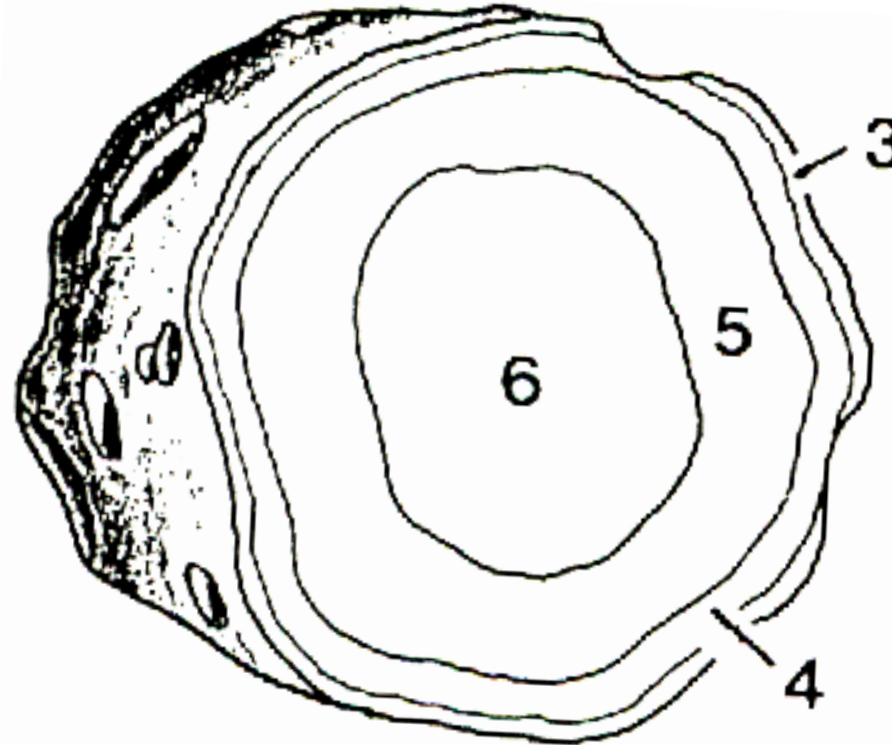


Taylor et al 1987

**However, thermal alteration evidence suggests that pre-collisional object had more of an onion shell structure**



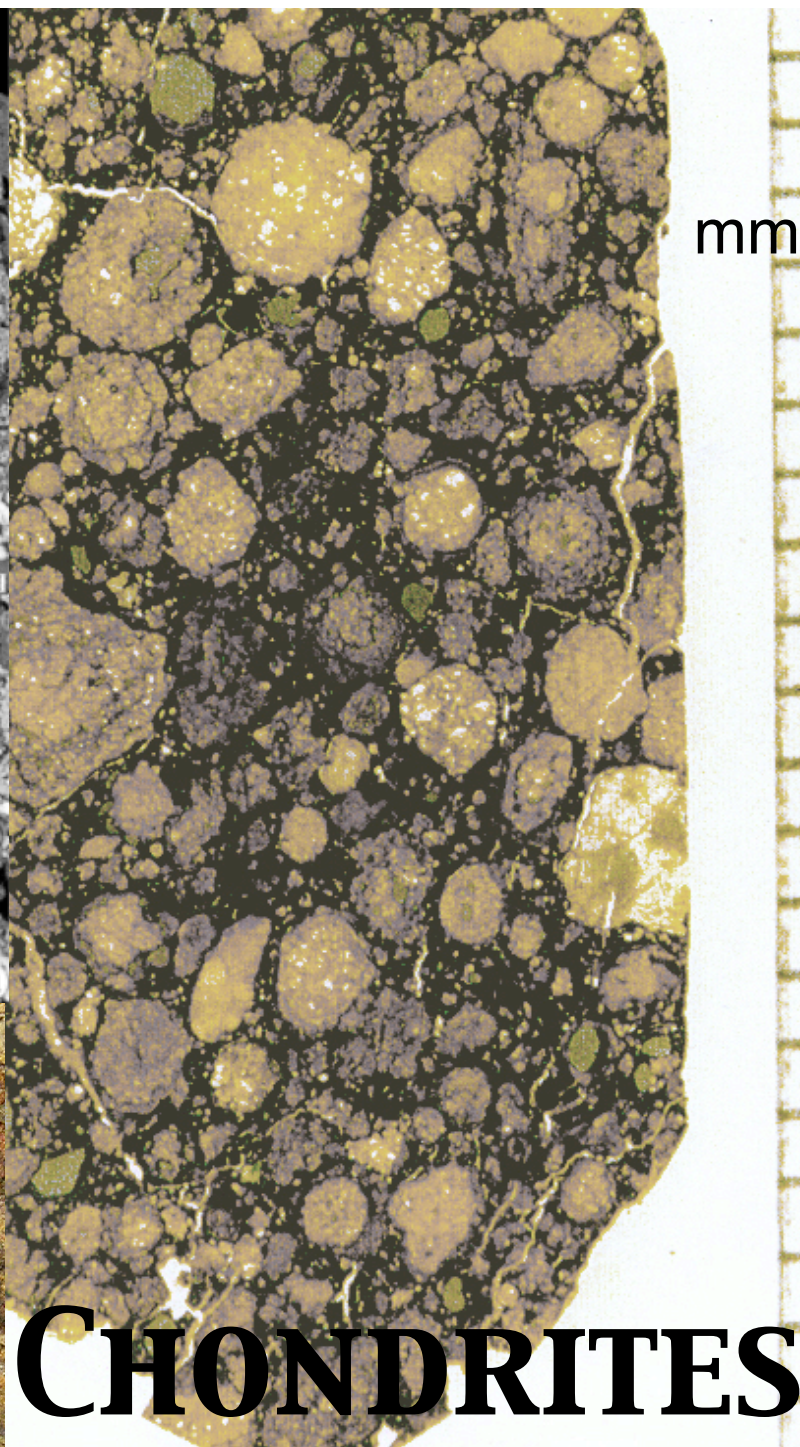
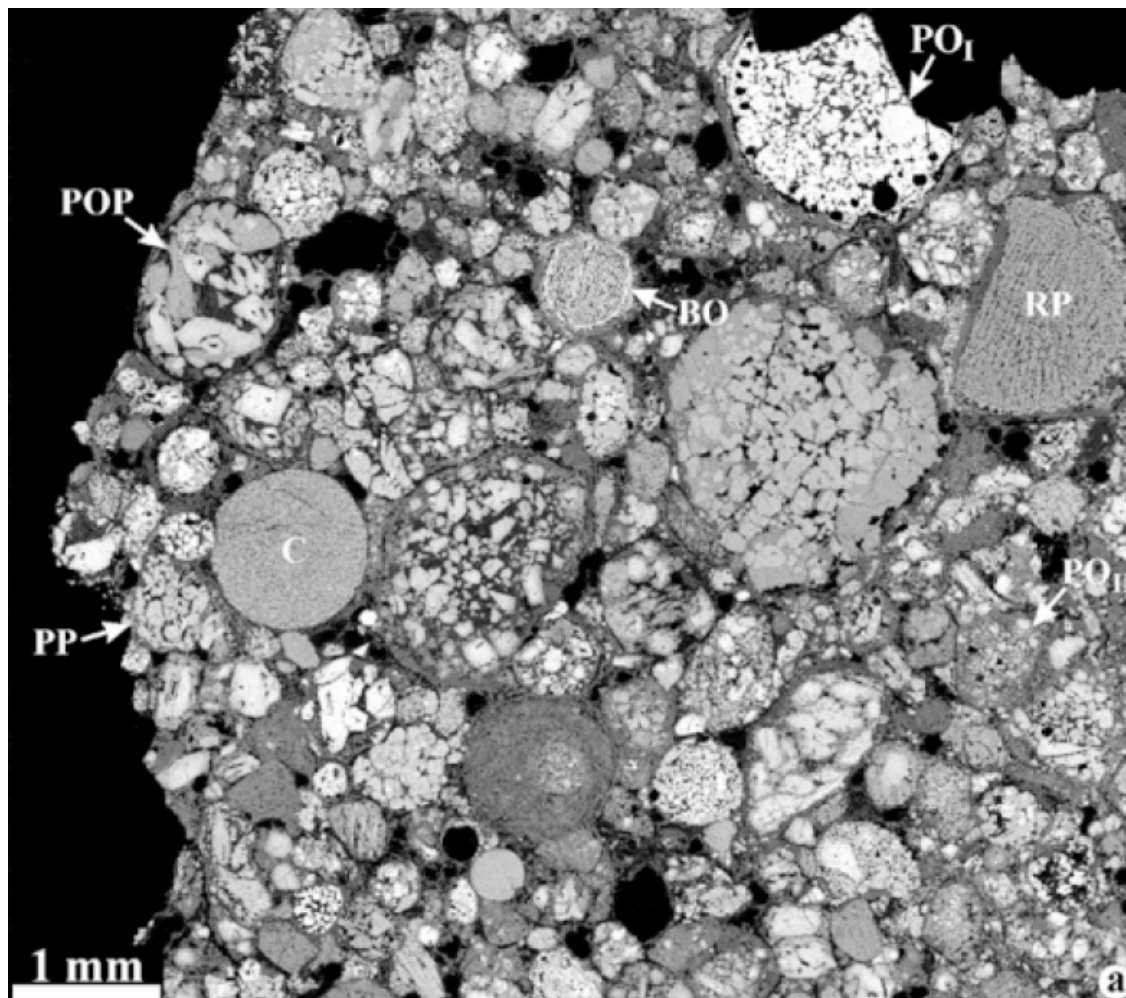
**Initial contents were very homogeneous;  
thermal alteration baked inner material the most**



Trieff et al 2003

**How to construct 100km asteroids (parents of groups)  
entirely out of “chondrules” with similar properties?**





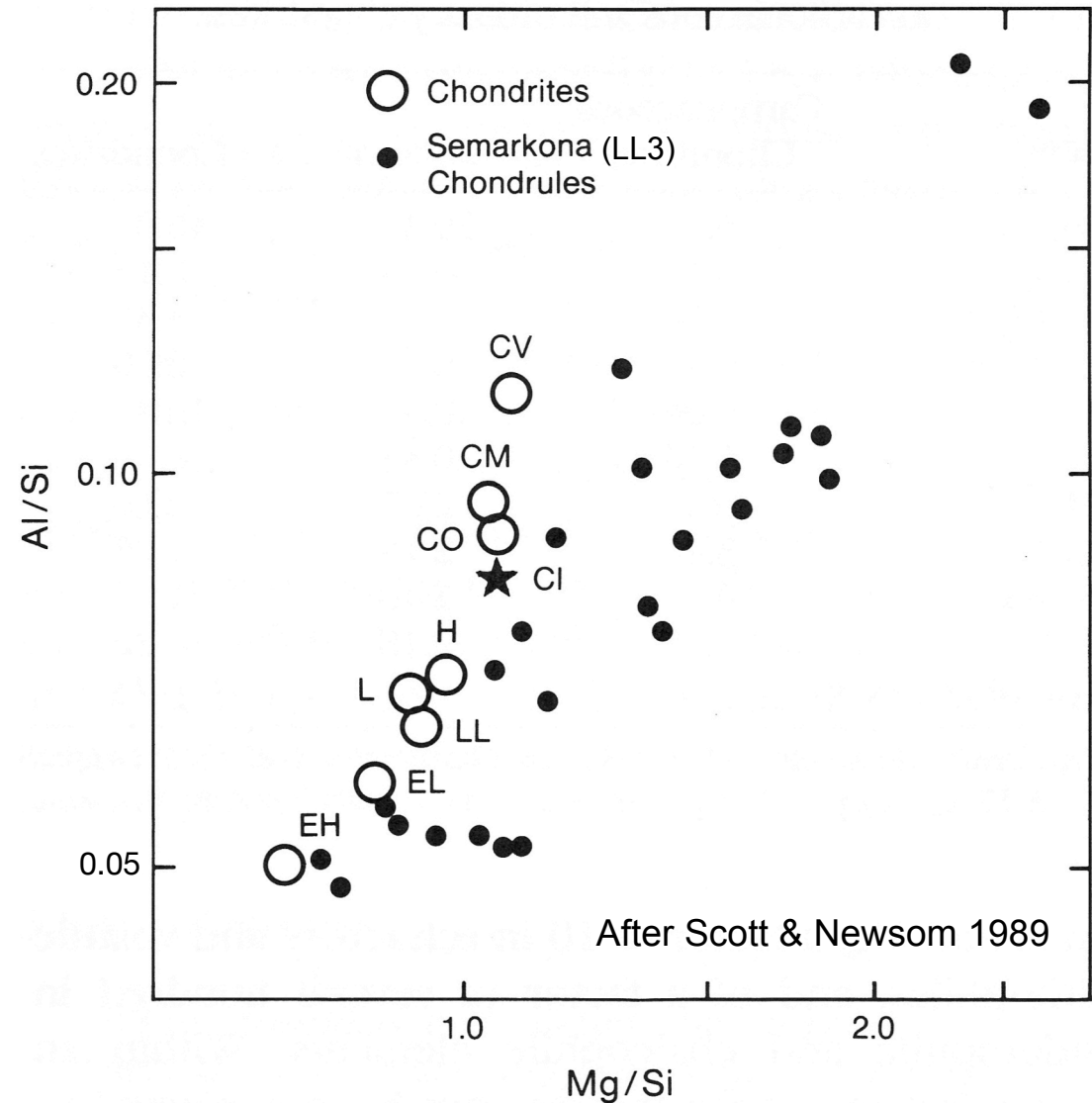
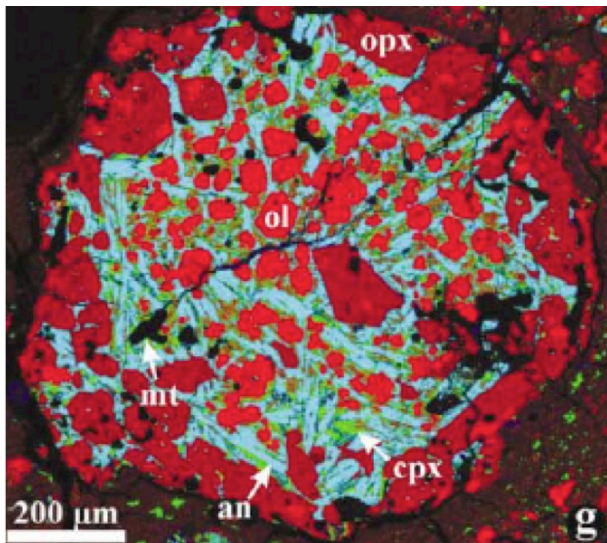


# What properties define chondrite *groups*?

## 1. Chemistry and mineralogy

Major element variance between chondrules in a given meteorite exceeds variance between all groups

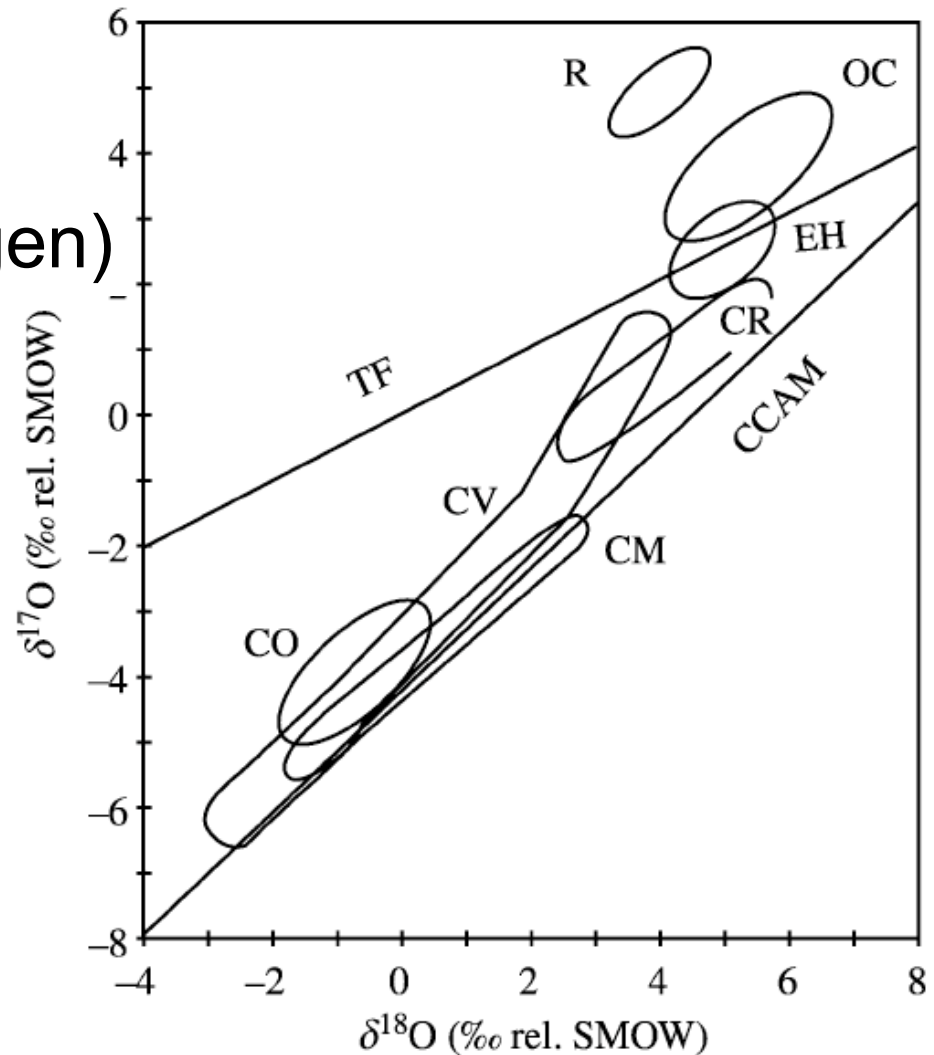
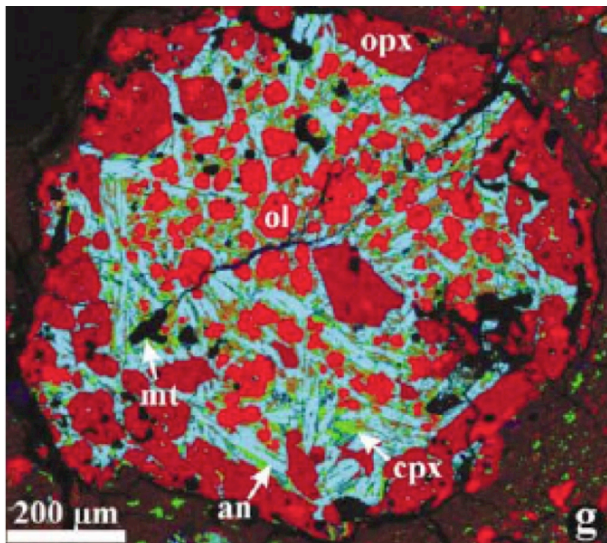
Groups represent “centroid” of a diverse local sample





## 2. Isotopes (here, oxygen)

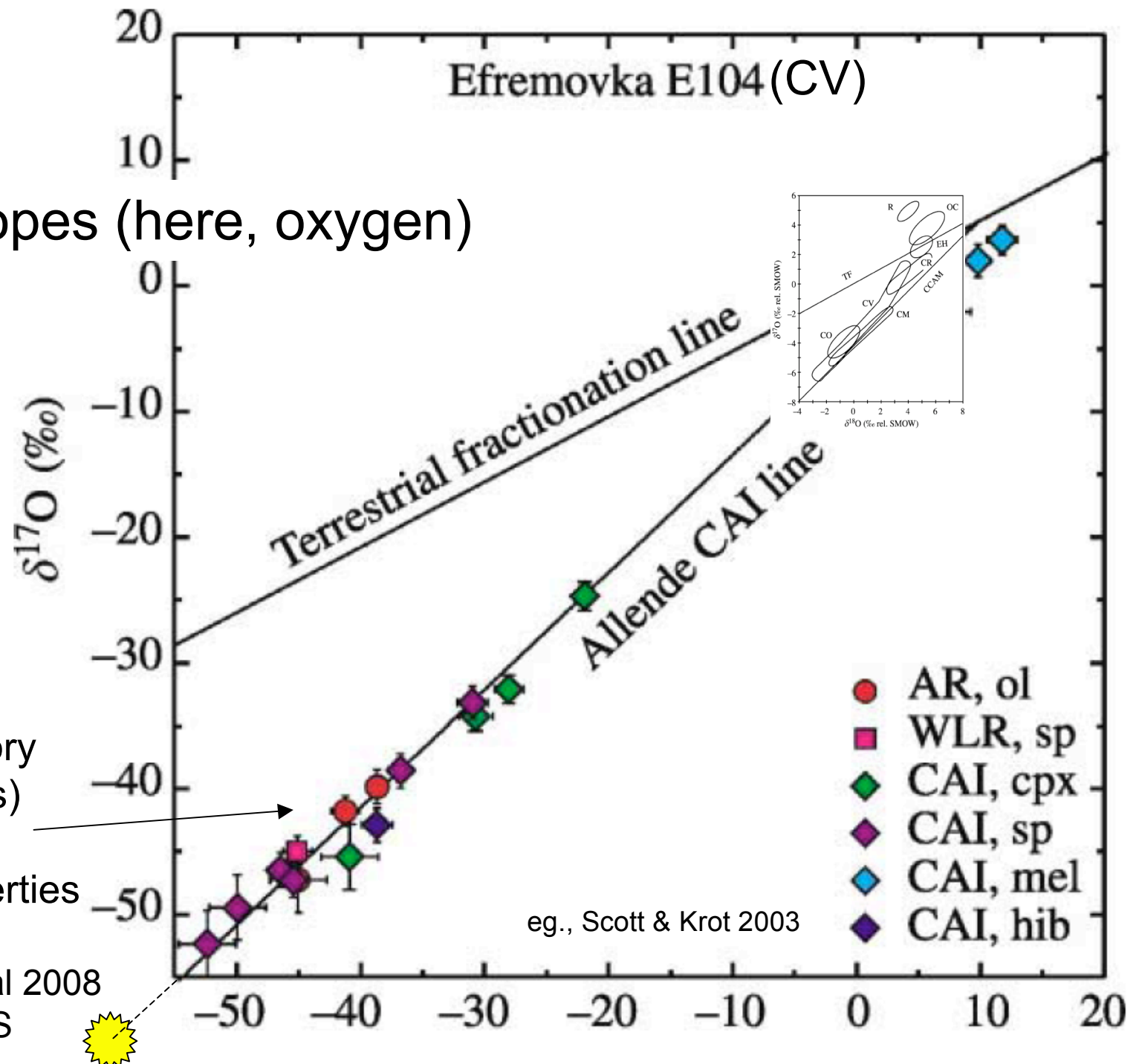
Isotopic composition of chondrules and bulk samples separate the different groups



eg., Clayton 1993 Ann Rev EPS



## 2. Isotopes (here, oxygen)





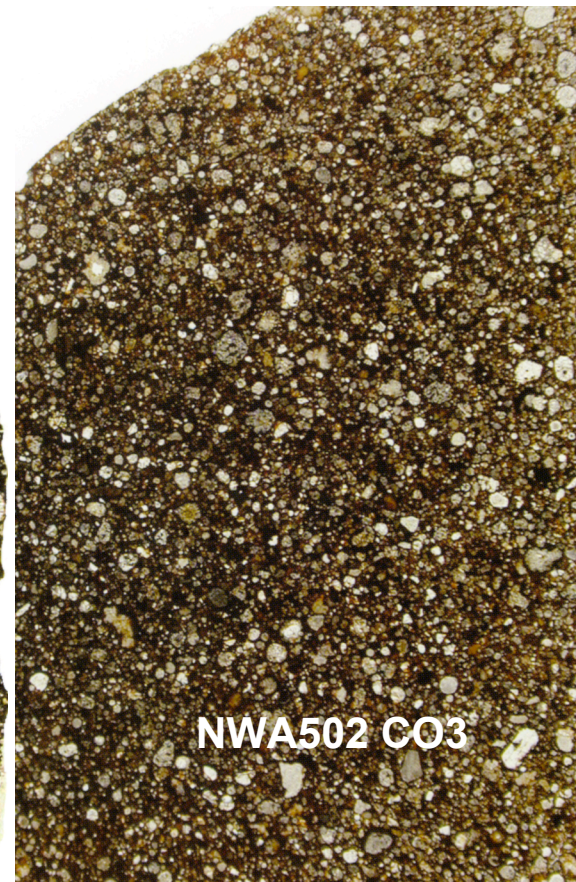
### 3. Particle size & dust content



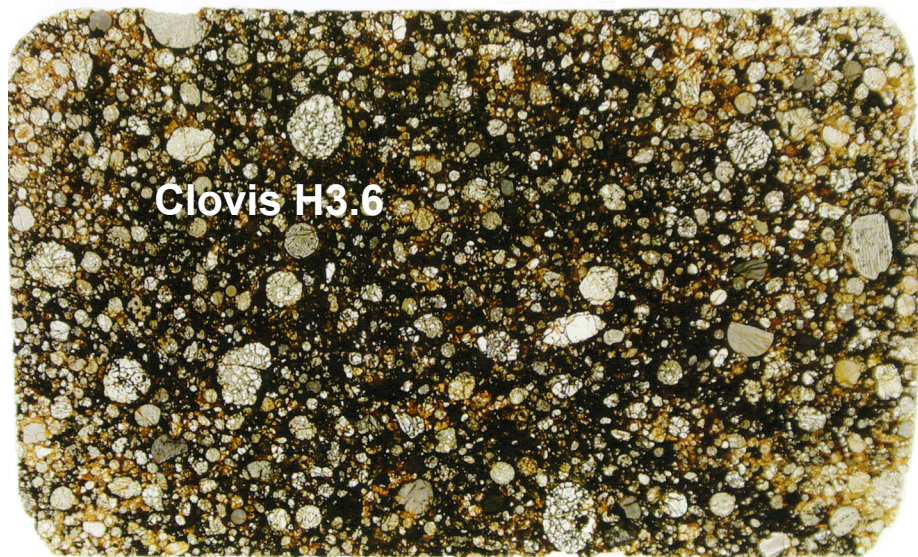
Murchison CM2



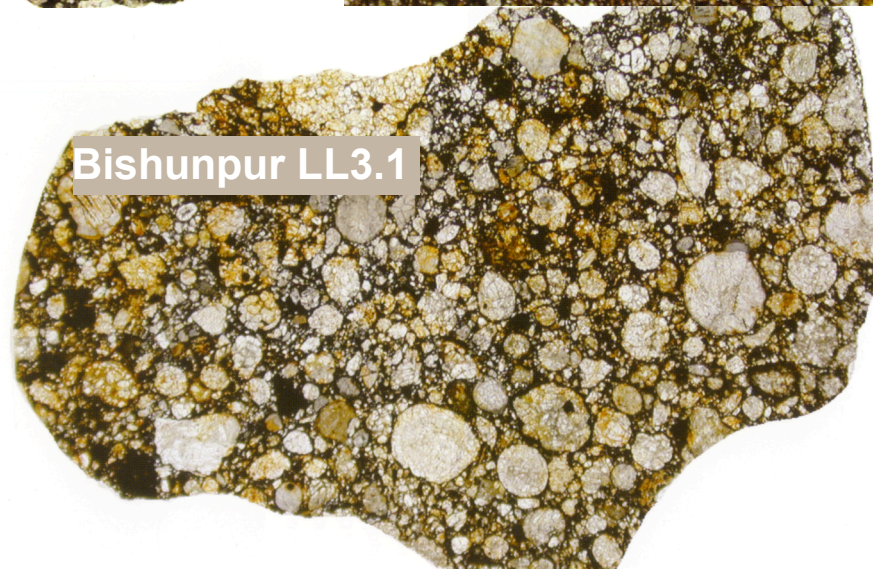
Vigarano CV3



NWA502 CO3



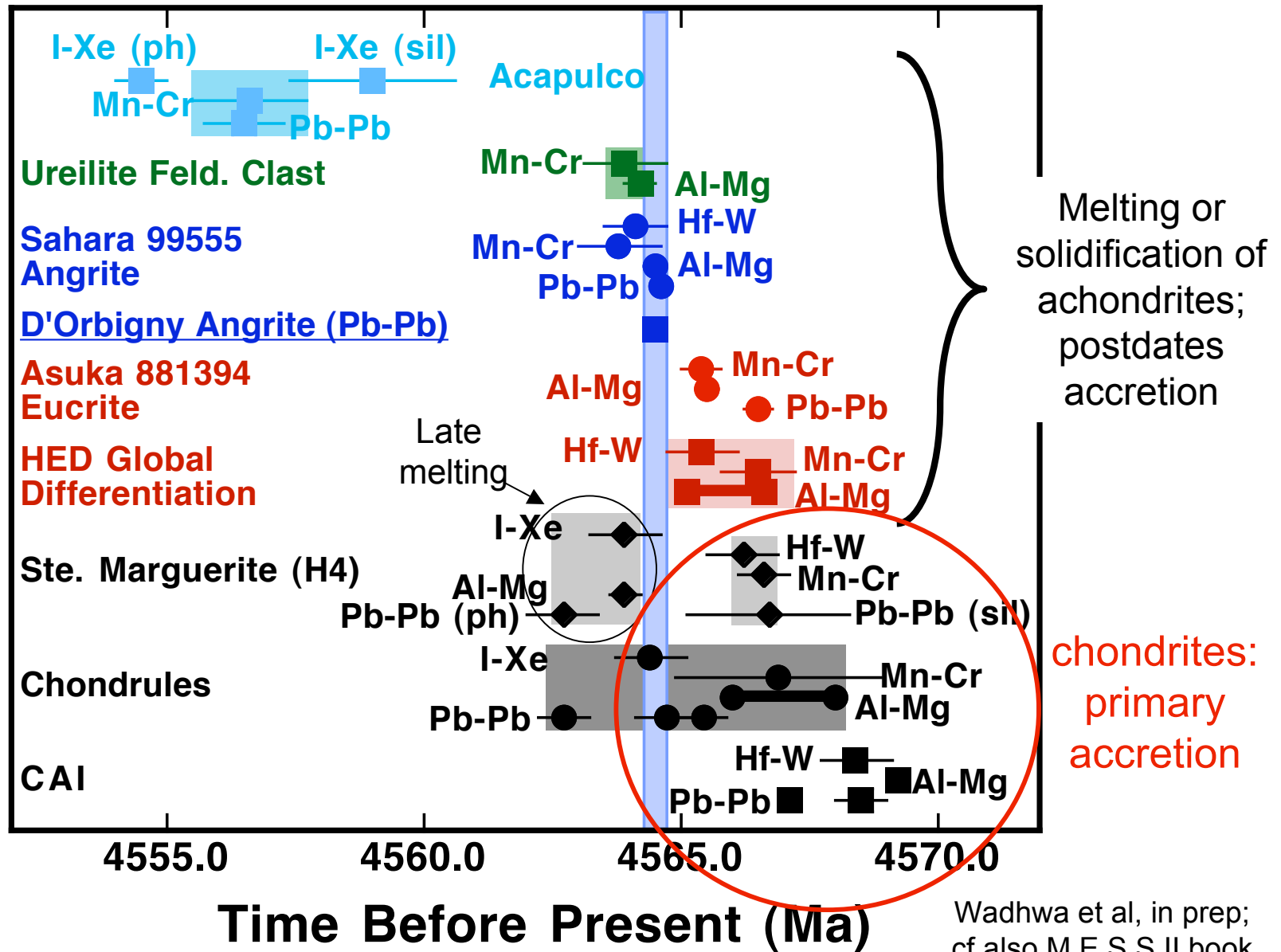
Clovis H3.6



Bishunpur LL3.1



# Short- and long-lived radiogenic isotopes for age dating



*Few Myr age difference even between particles in the same rock!*



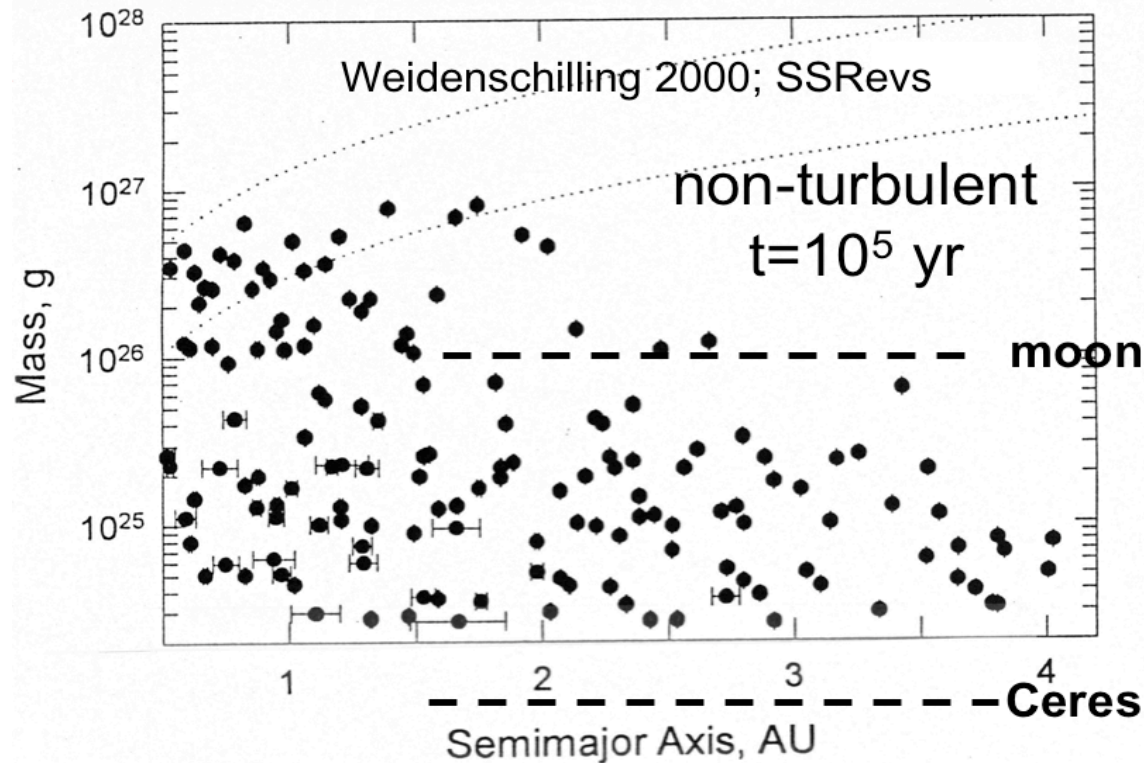
## Primary Accretion was *INEFFICIENT*

Non-turbulent models lead to rapid growth in dense midplane

*but* isotopic age dating shows formation spanned several Myr

Anything >20km forming in first Myr melts from  $^{26}\text{Al}$  decay

*but* melted asteroids are rare



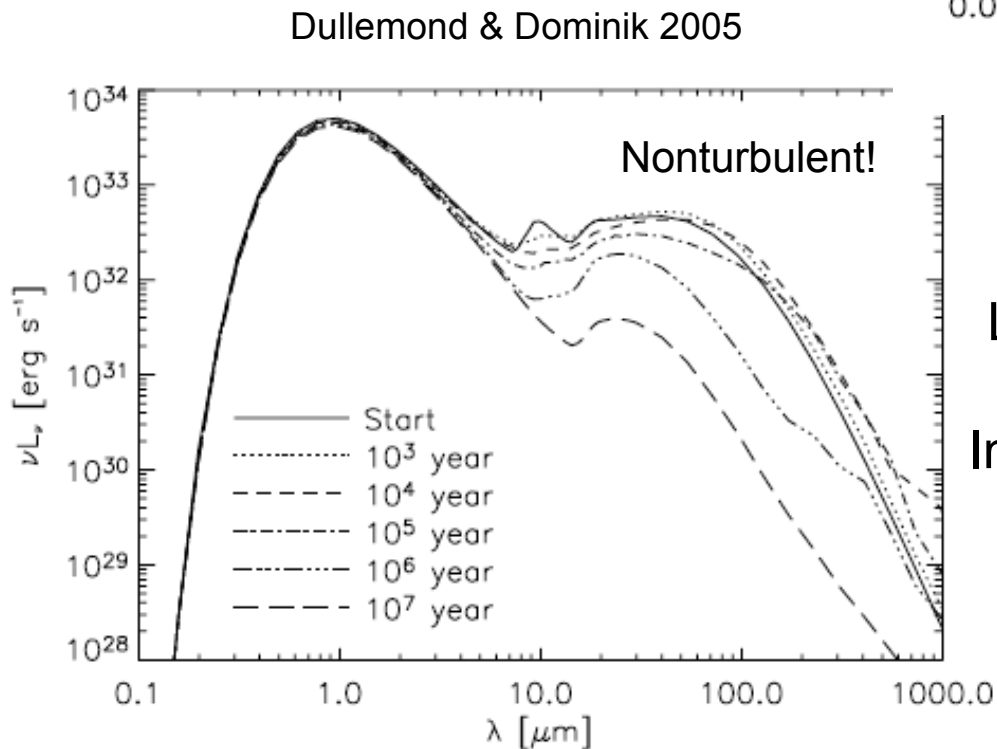
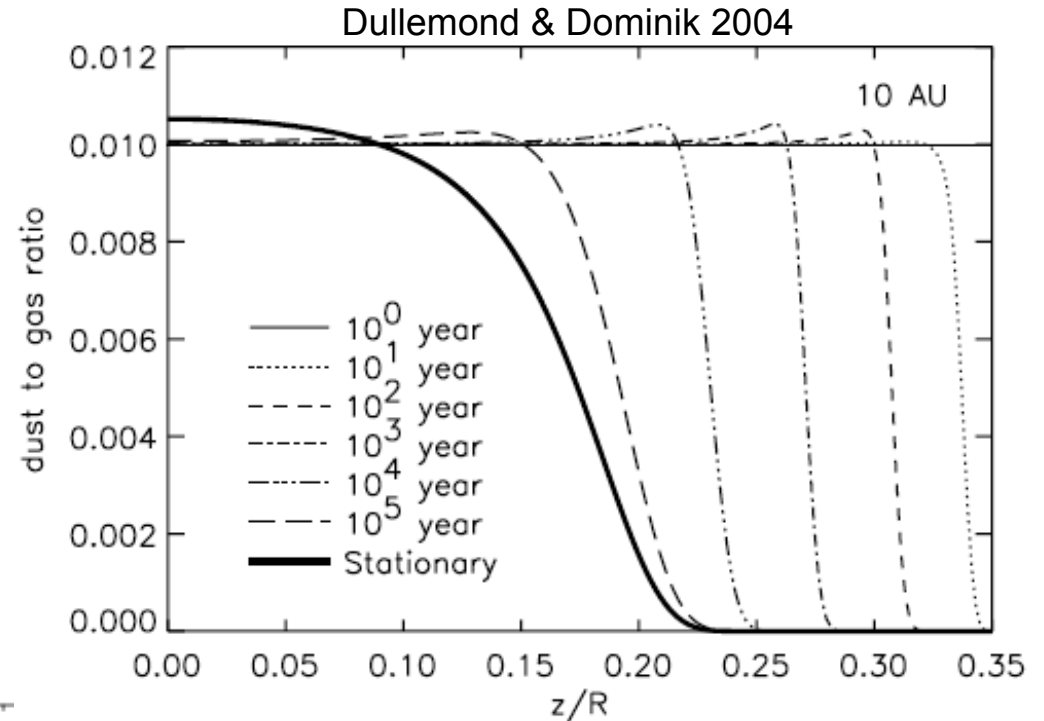
## *Turbulence can delay primary accretion*

Few % of accretion energy from  $10^{-8} M_{\text{sun}}/\text{yr}$  maintains  $\alpha = 10^{-4}$  or so



# Some observations favor turbulence

Weak turbulence can maintain small grains at observed altitudes forever, in the absence of growth



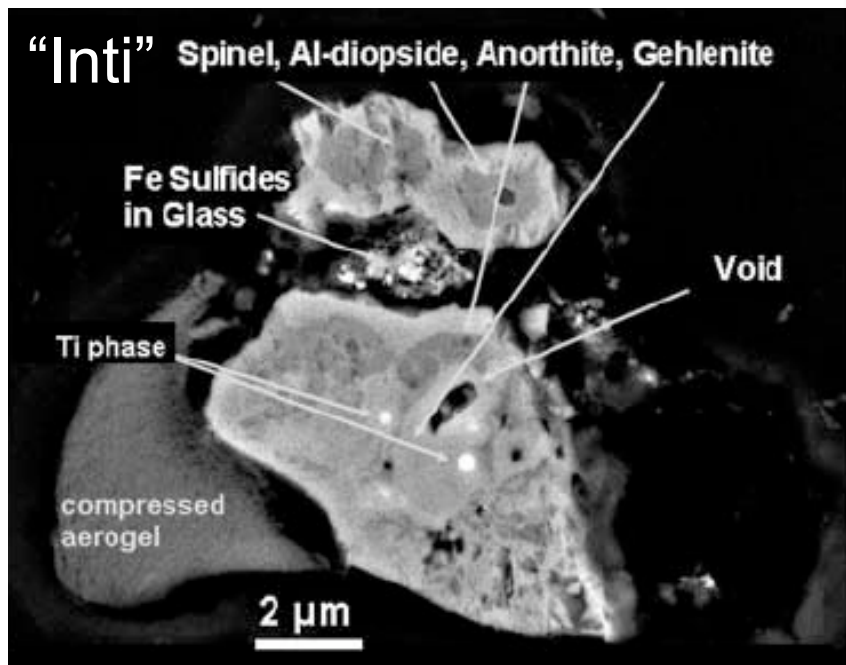
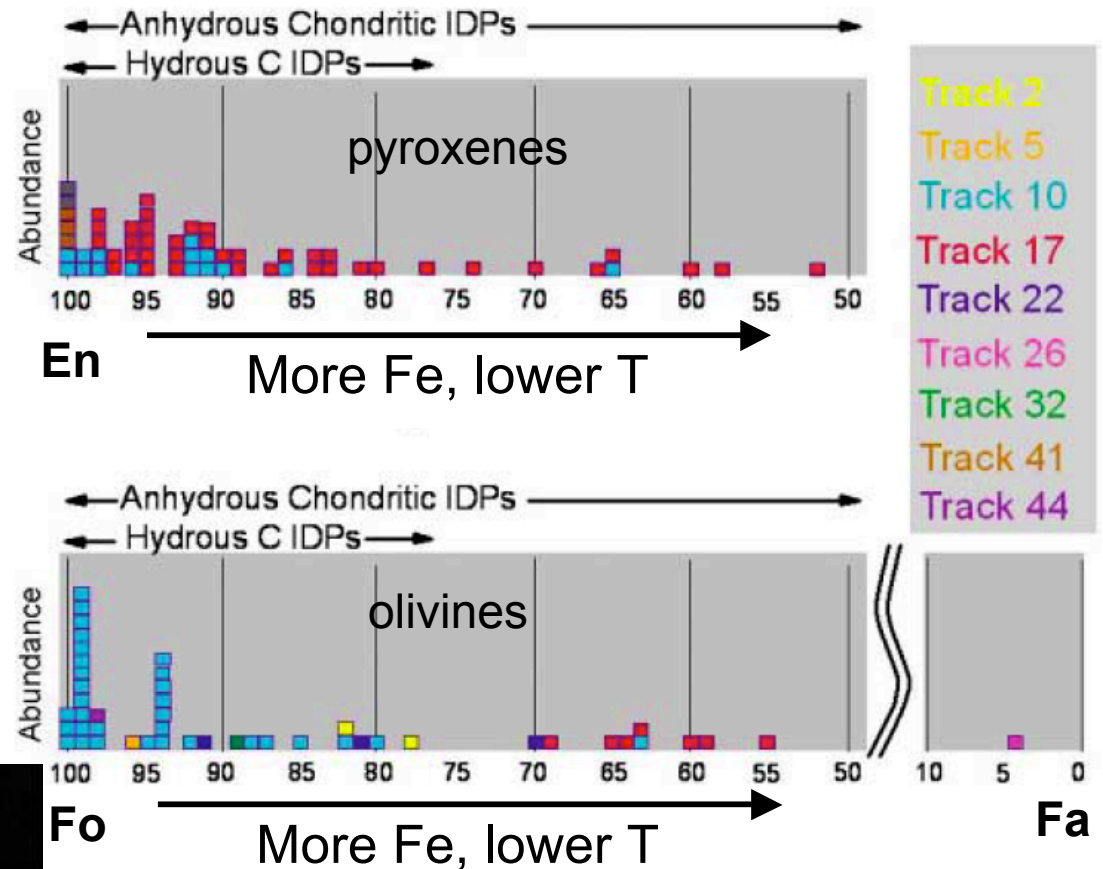
Low relative velocities ensure sticking;  
rapid growth leads to settling.  
Implies ongoing large-particle collisions  
AND turbulent transport of dust  
back to high altitudes



**STARDUST:**  
 nm- $\mu$ m grains;  
 (CAI, Fe-Mg silicates);  
 crystallines abundant

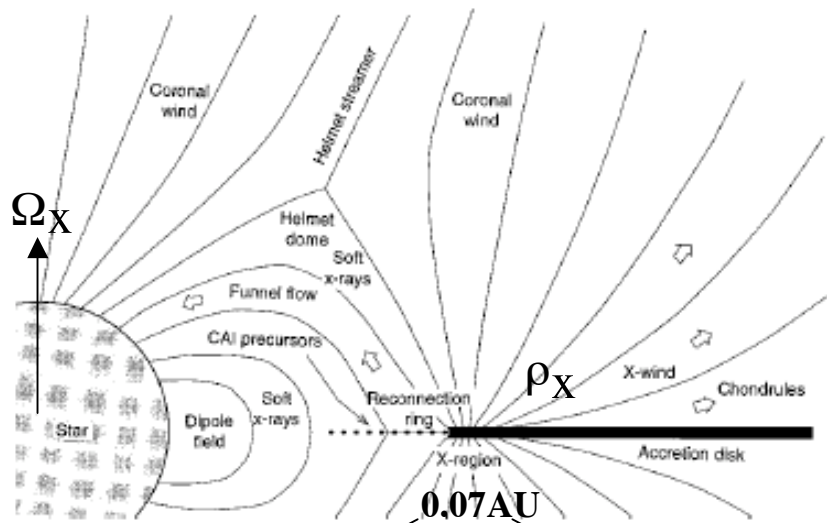
Zolensky et al Science 2006

Brownlee et al Science 2006

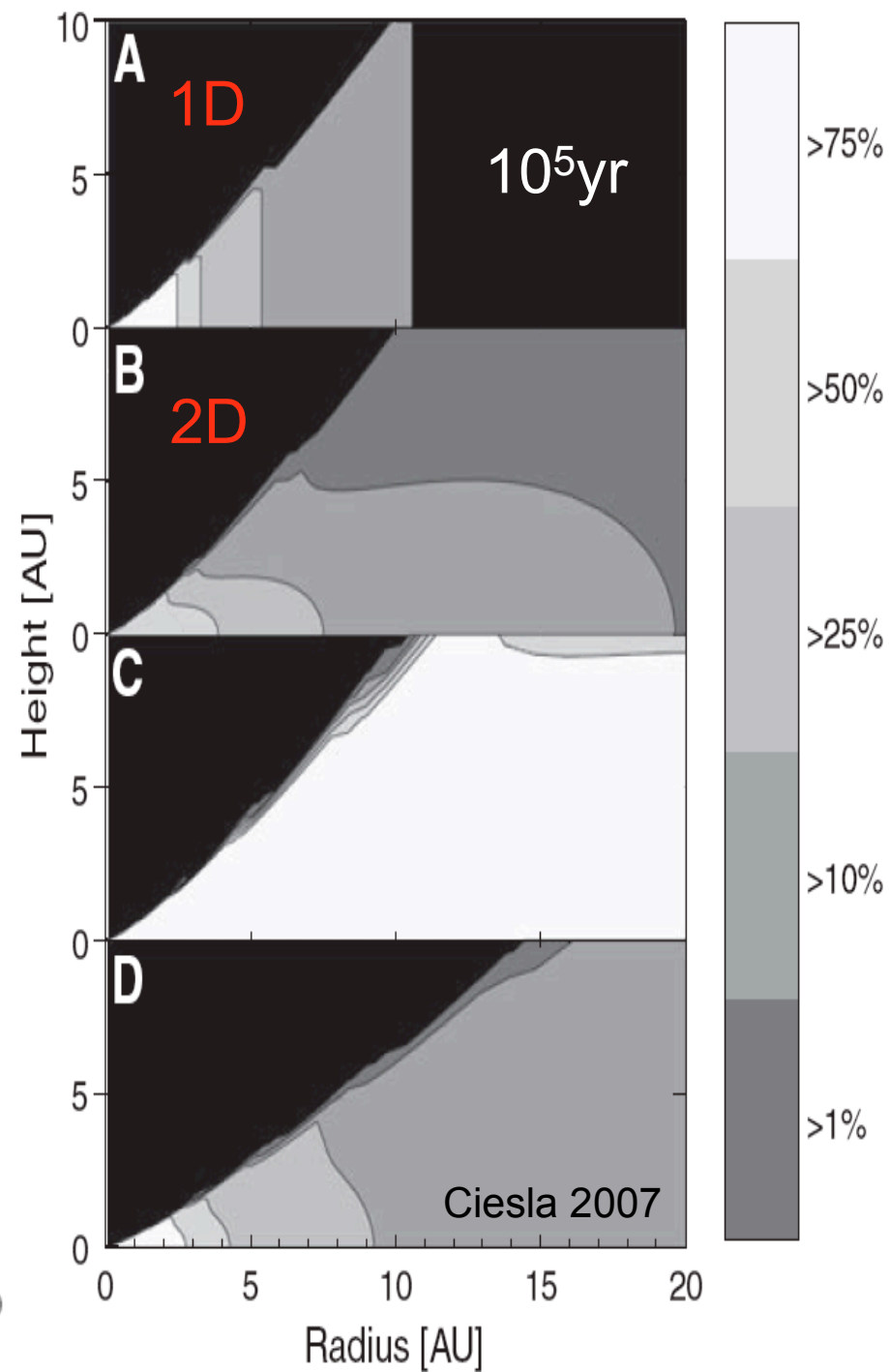
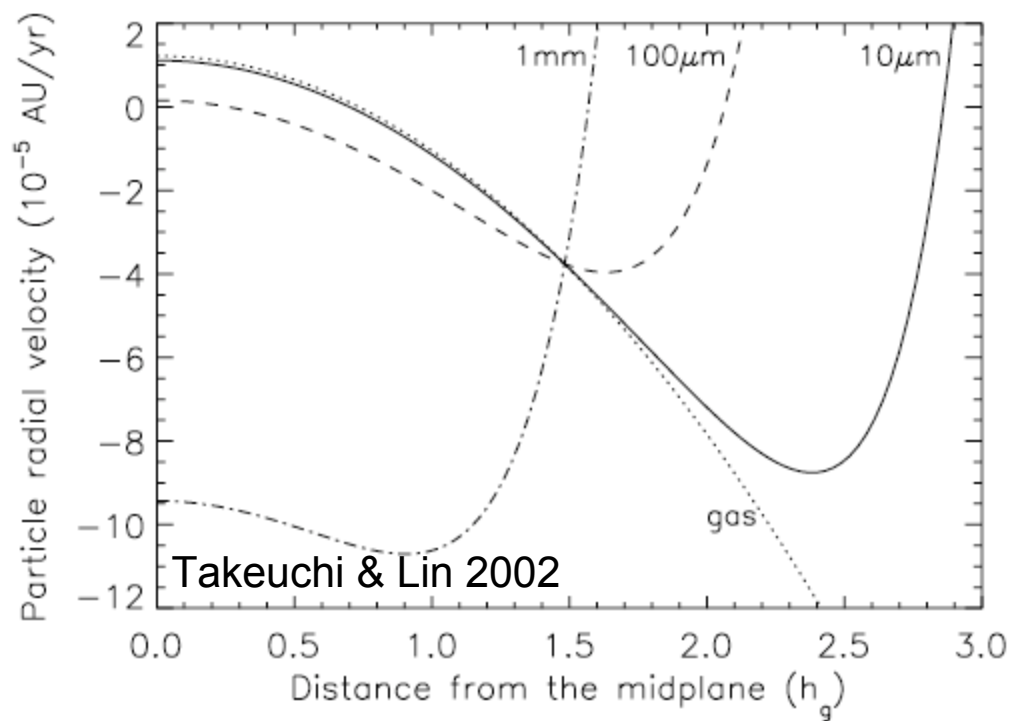


*STARDUST team concludes:  
 Vigorous radial transport  
 from inner to outer nebula,  
 sampling a wide variety  
 of formation conditions*



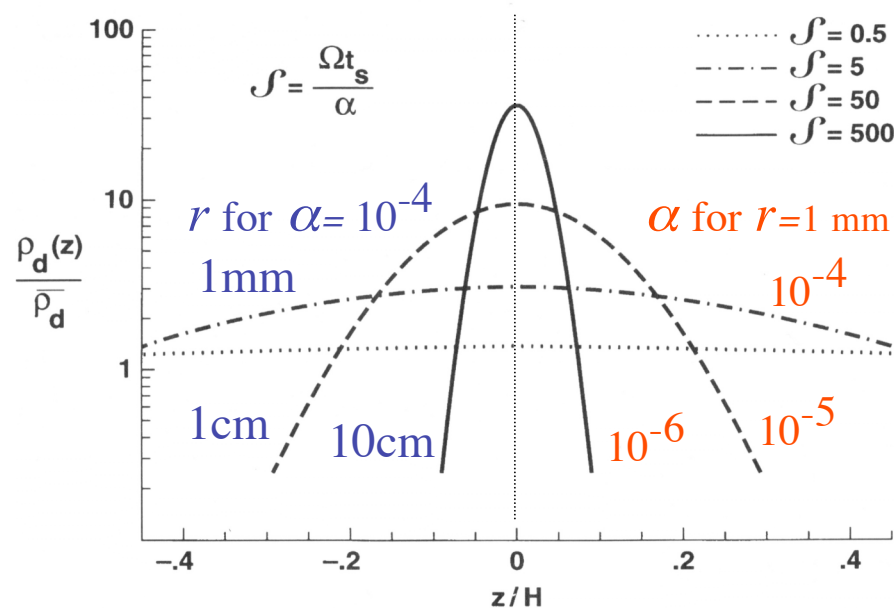


Shu et al 1996, 1997 Science **fluctuates**  
 Liffman & Brown Icarus 1995





# Turbulence keeps midplane densities low



Turbulence diffuses particles vertically, preventing “settling to the midplane” even after some growth has occurred

Adapted from Dubrulle et al 1995

## Various *midplane instabilities* proposed over the years

(Safronov 1960, Goldreich & Ward 1973, Sekiya 1998 et seq;  
Goodman & Pindor 1995; Youdin and Shu 2002 et seq;

are precluded by global turbulence at levels  $\alpha \ll 10^{-2}$

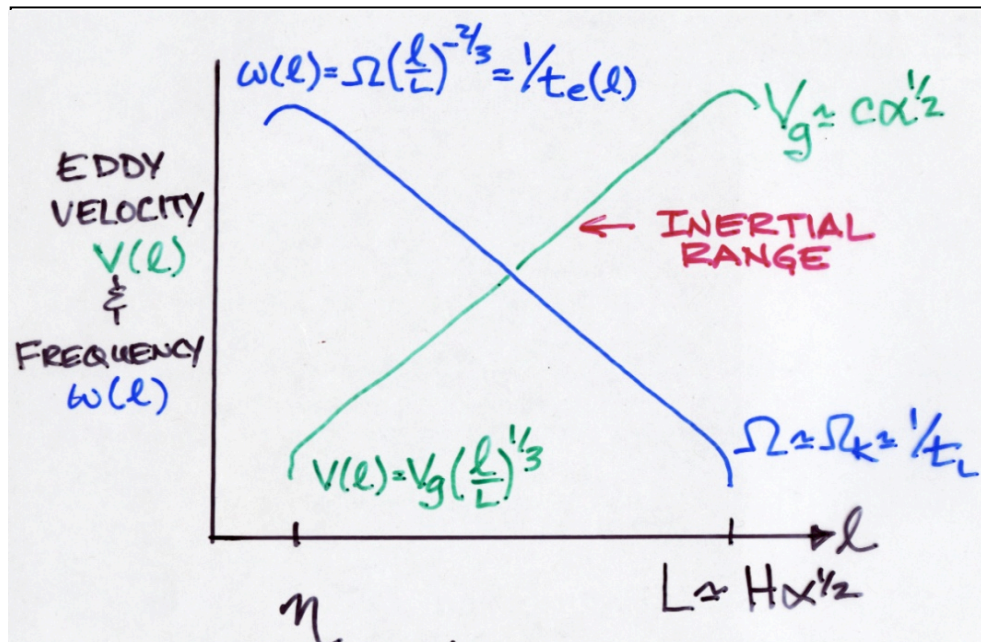
-and-

In nonturbulent nebulae, growth by sticking in dense midplane layers is already (too) rapid even without instabilities.

cf. reviews by Cuzzi & Weidenschilling, Met. Early Sol Syst II (2006); Dominik et al PPV (2007)



# Gas turbulence drives particle velocities



Large eddies contain most of the energy,  
large eddy velocity  $V_g \sim c \alpha^{1/2}$ .

Large eddy frequency  $\sim$  the orbit freq;  
Small eddies have faster overturn times

Particle relative velocities can be  
calculated for any turbulent intensity

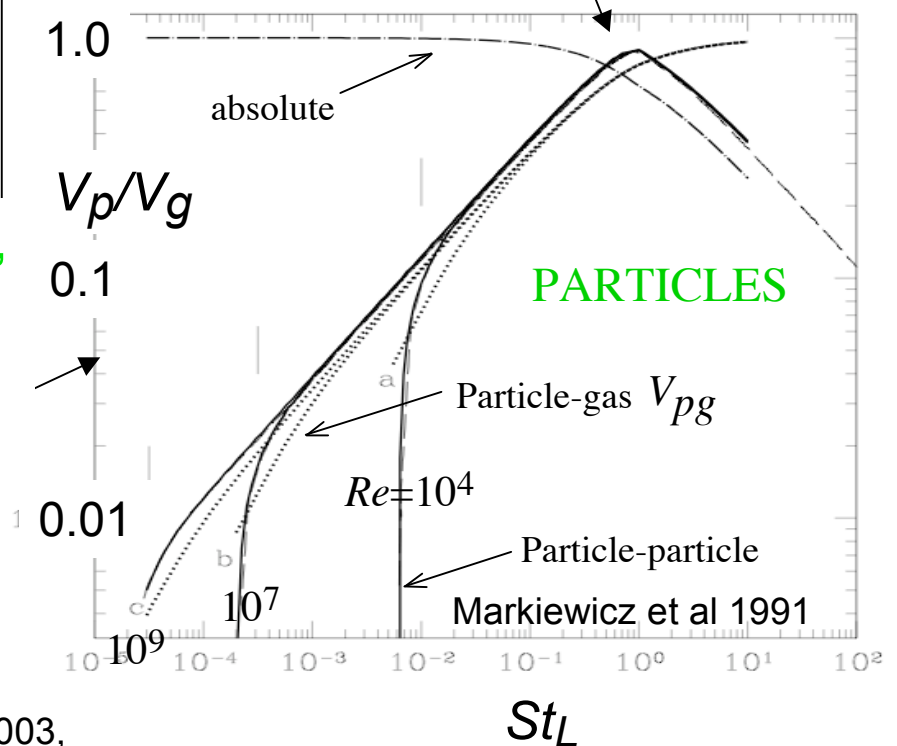
Particle stopping time

$$t_s = r \rho_s / c \rho_g$$

(expr. changes for  $r >$  gas mfp)

Peak velocities for particles with  $t_s$   
comparable to large eddy time

$$(St_L = t_s \Omega_L = 1)$$



Völk et al 1980, Markiewicz et al 1991, Cuzzi and Hogan 2003,  
Ormel and Cuzzi 2007, Youdin and Lithwick 2007, Carballido et al 2006,2008

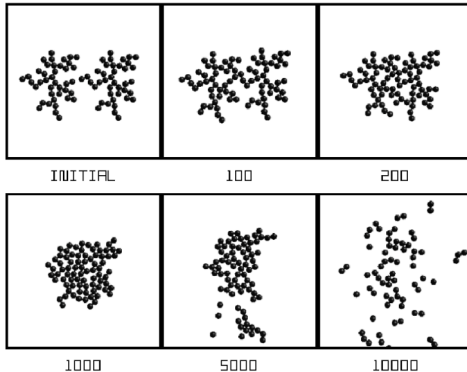


# Sticky business

Critical “sticking” velocity varies with material and monomer size

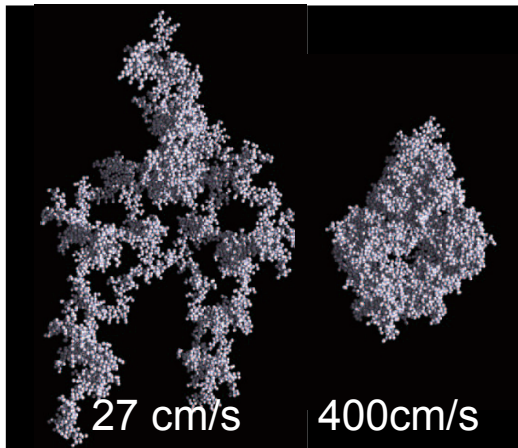
(J. Blum, this mtg)

Sticking is fairly robust, up to (deci?)meter-size



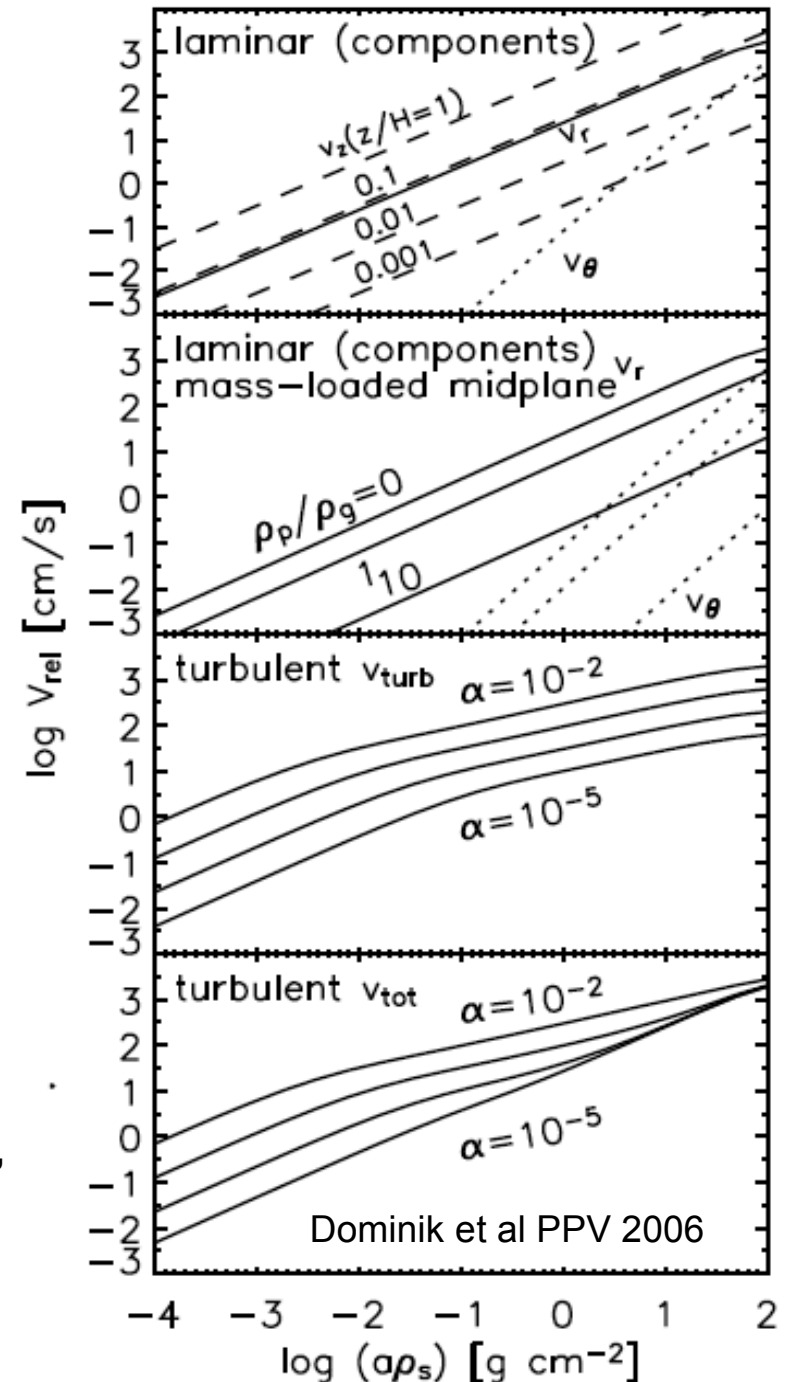
Dominik & Tielens 1997

2D; 3 regimes depending on critical energies  $E_{roll}$ ,  $E_{stick}$



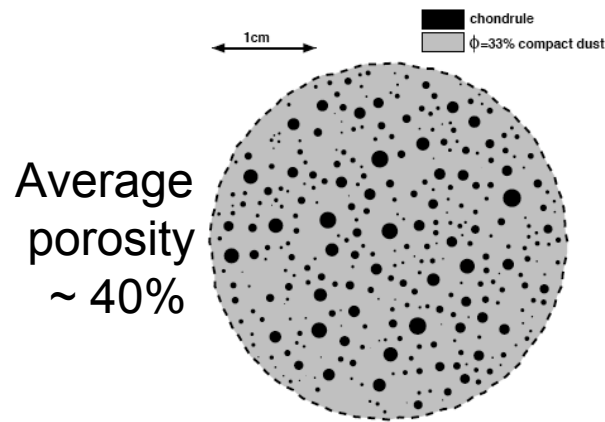
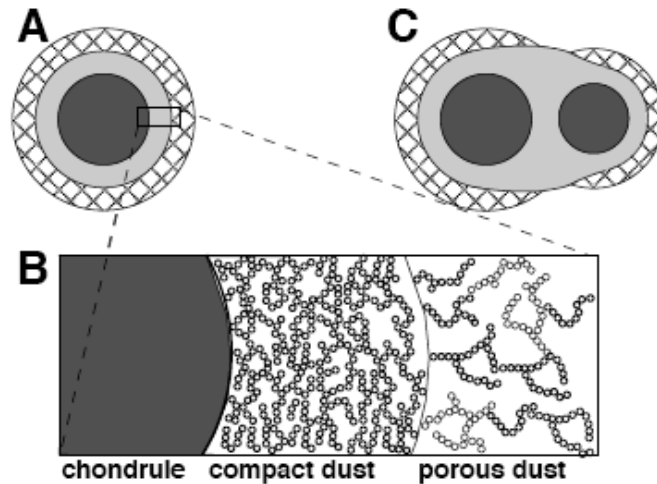
Suyama et al 2008, Wada et al 2008 (LPSC)

3D; compaction & sticking up to 4m/s (high for aggregates, maybe relevant for chondrule rims)





# Small particle growth theory (Dominik & Tielens 97, Ormel et al 2008 ApJ in press)

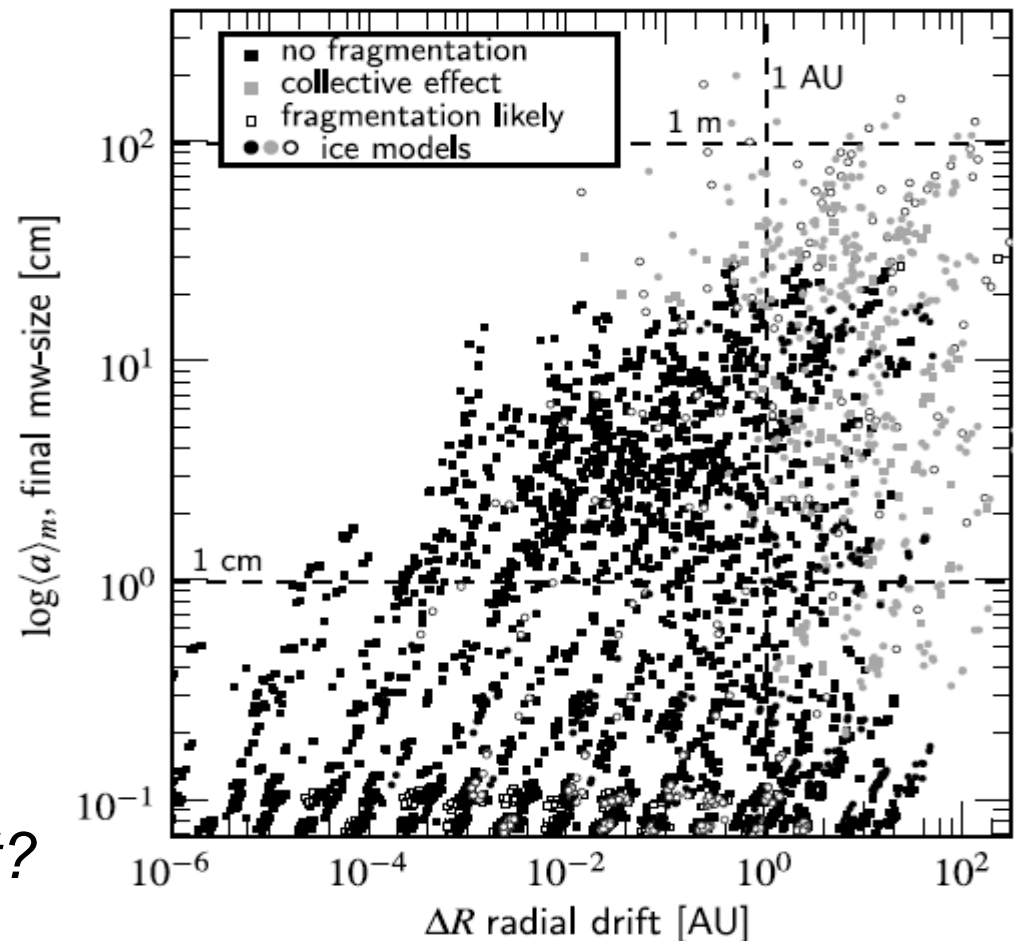


$$E_{\text{coll}} > N E_{\text{roll}} \rightarrow \text{bounce}$$

$$E_{\text{coll}} > 10 N E_{\text{stick}} \rightarrow \text{fragment?}$$

$$E_{\text{stick}} = A_{\text{stick}} \frac{\gamma^{5/3} a_{\mu}^{4/3}}{\mathcal{E}^{2/3}}$$

$$E_{\text{roll}} = 6\pi^2 \xi_{\text{crit}} a_{\mu} \gamma = A_{\text{roll}} \xi_{\text{crit}} a_{\mu}'$$

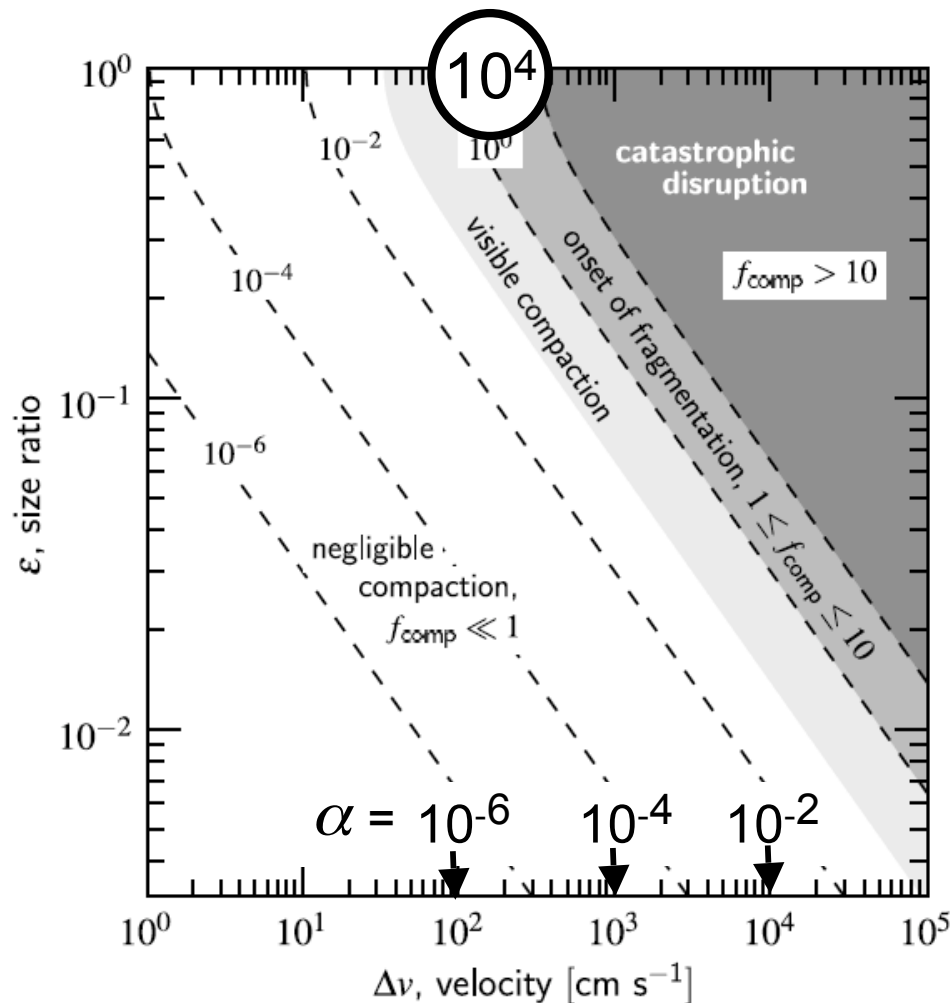




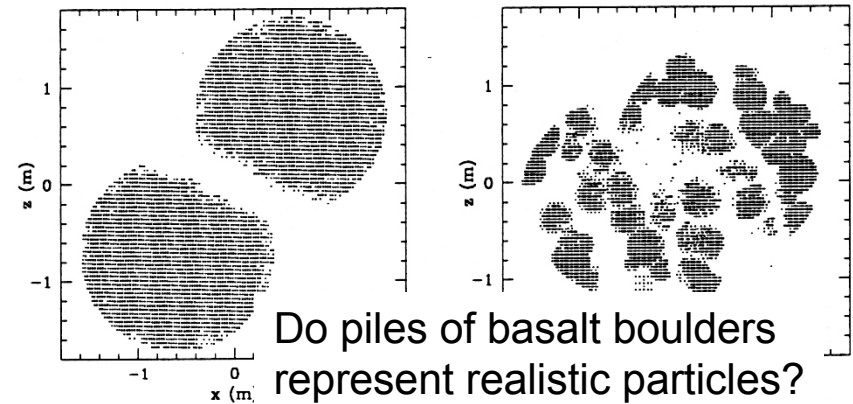
# What are the disruption strengths of m-size particles?

$$Q^* \sim v^2 \text{ for } m_1 \sim m_2$$

Ormel et al (2008) ApJ in press

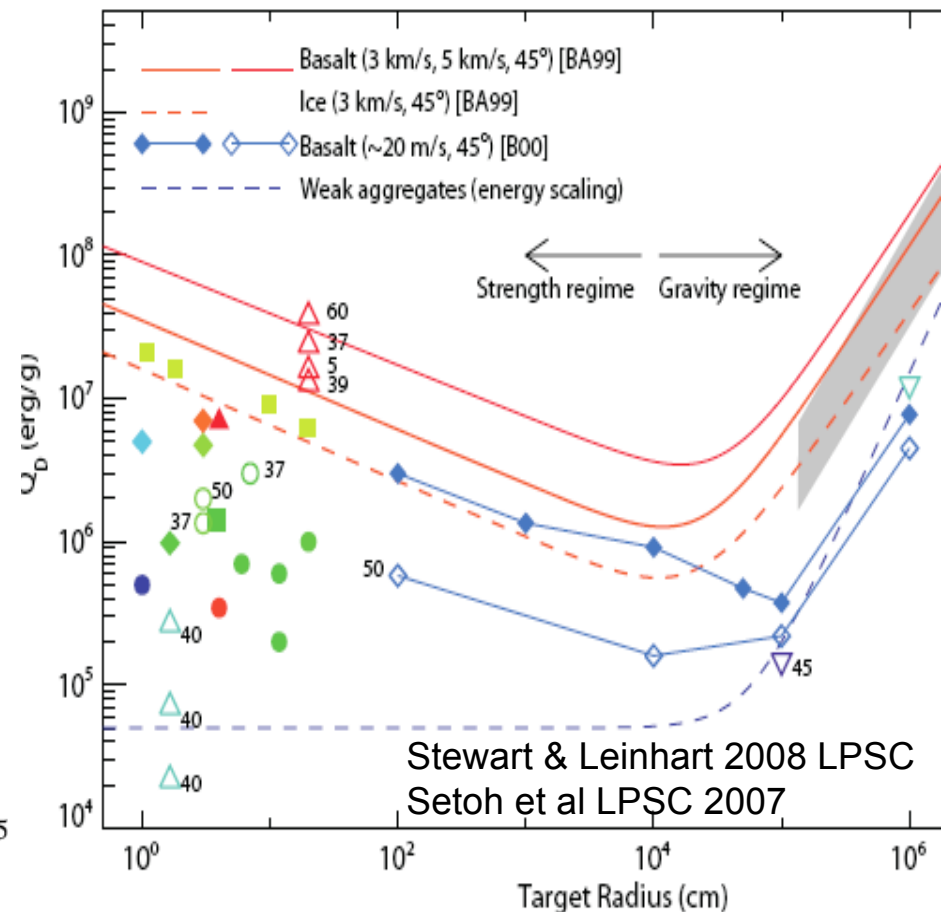


Benz 2000 Sp Sci Revs



Do piles of basalt boulders represent realistic particles?

B.





## SPH simulations (Sirono 2004 Icarus)

Conditions for collisional growth of a grain aggregate

443

$V = 10 \text{ m/s}$   
normalized compressive  
and tensile strengths  
 $(\Sigma_o, T_o) \sim 10^{-2}, 10^{-3}$   
of solid, or  
(8000, 70000) dyn/cm<sup>2</sup>

Projectile here is much  
smaller than target;  
equal mass would  
provide 30x larger  
energy, suggesting  
5-6 x smaller  $V_{\text{crit}}$ ;  
again  $\sim 1-2 \text{ m/s}$

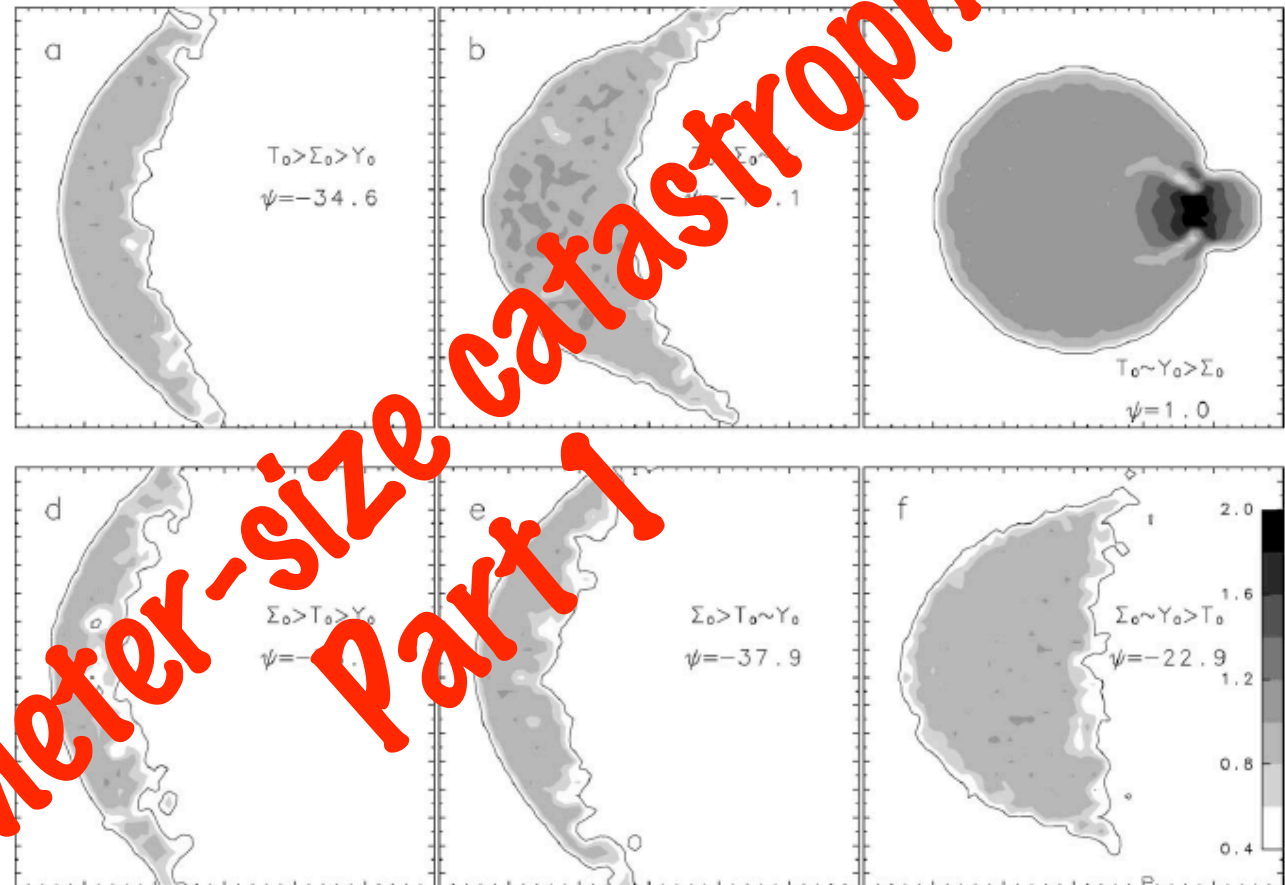


Fig. 13. Results of collisions having various orders of compressive, tensile, and shear strengths. Sticking takes place only if the compressive strength is the lowest among the three components (panel c).

**And**, Langkowski et al 2007  
find  $(\Sigma_o, T_o) \sim 2000-10000 \text{ dyn/cm}^2$

*Collisions may preclude growth  
past around meter-size*



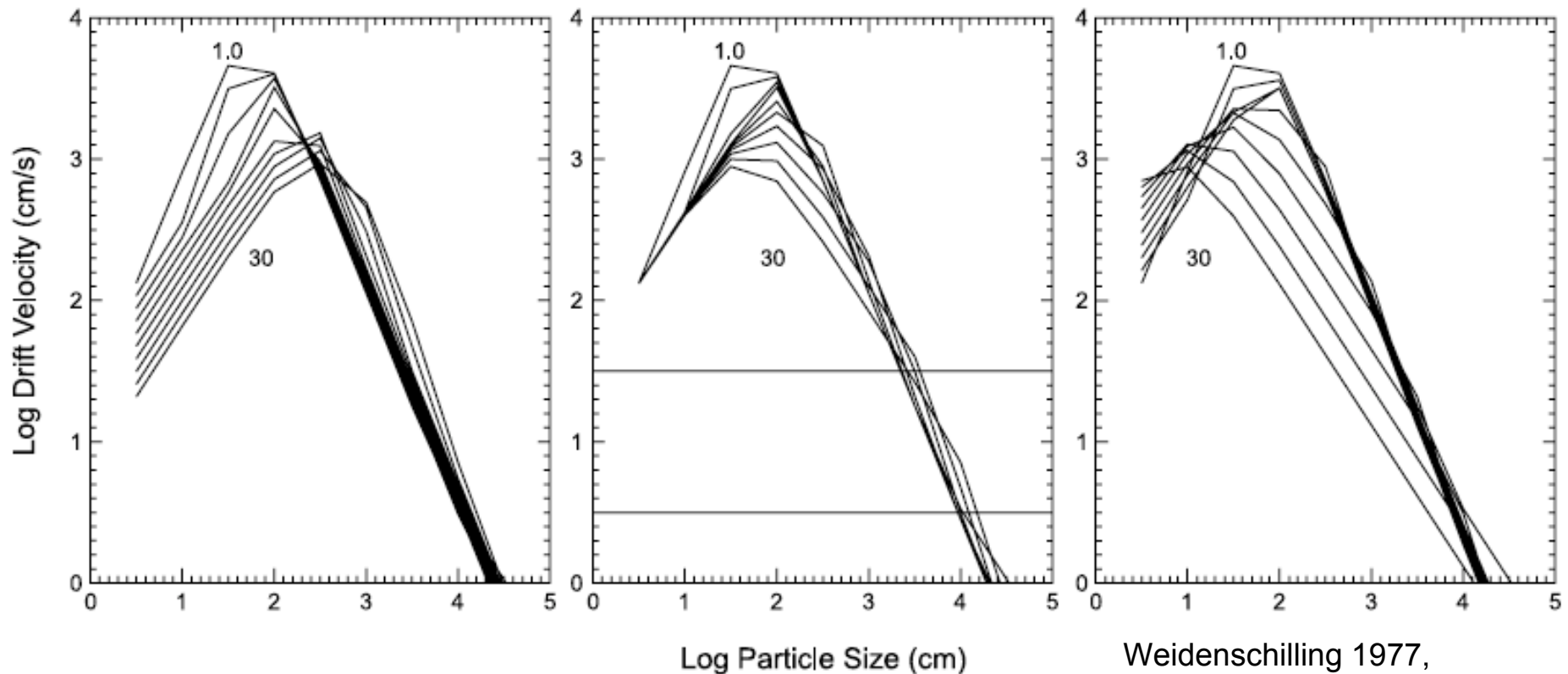
# Transport of solids by inward radial drift (gas drag)

On average,  $dP/dr = -\beta R\Omega^2$  near midplane

Gas orbits slower than keplerian, so particles incur headwind and lose angular momentum

Peak radial drift speed  $V_D = \beta V_K \sim 1$  AU/century

Reduced in dense midplane layers (if non-turbulent)



Weidenschilling 1977,  
Cuzzi & Weidenschilling 2006



# Particles accumulate in radial pressure maxima

Haghigipour and Boss 2003a,b; Rice et al 2004

also Johansen et al 2006, 2007

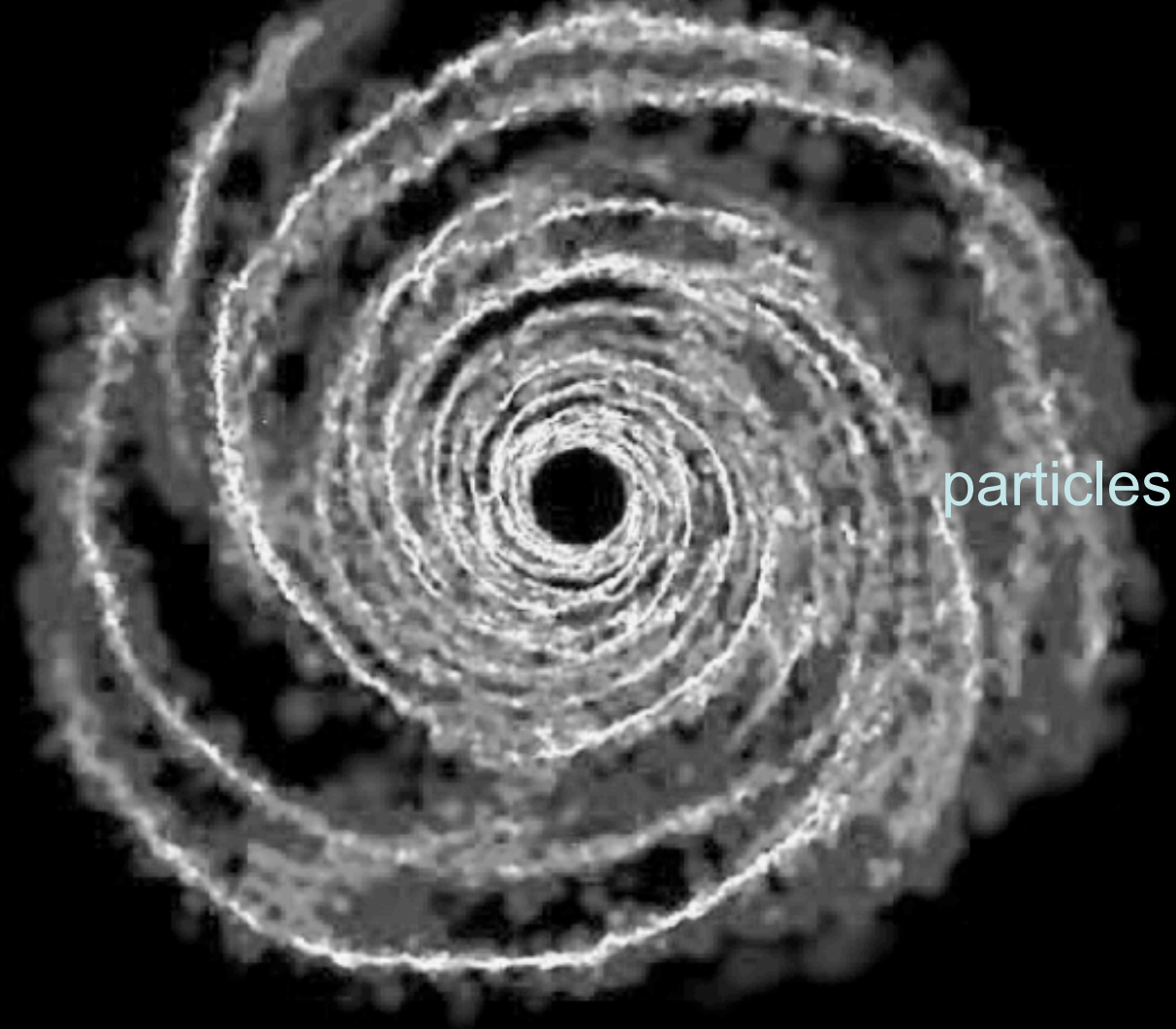




# Particles accumulate in radial pressure maxima

Haghigipour and Boss 2003a,b; Rice et al 2004

also Johansen et al 2006, 2007



particles

But - effect only reduces radial drift by half or so (Johansen et al 2006)



## “Radial drift barrier”

Particle has to be able to grow before leaving its environment

$$t_{res} = a/\dot{a} > r/\dot{r} = t_{gro}$$

$$\dot{a} = \beta V_K(r/1\text{m}) = \beta \Omega (r/1\text{m}), \text{ where } \beta \sim 10^{-3}$$

$$\dot{r} = \dot{m}/(4\pi r^2 \rho_s) = \Delta V \rho_{loc}/\rho_p, \text{ where } \Delta V \sim \text{few m/s}$$

$$(r/1\text{m})^2 \leq \Delta V (\text{m/s}) (\rho_{loc}/\rho_p) / \beta \Omega$$

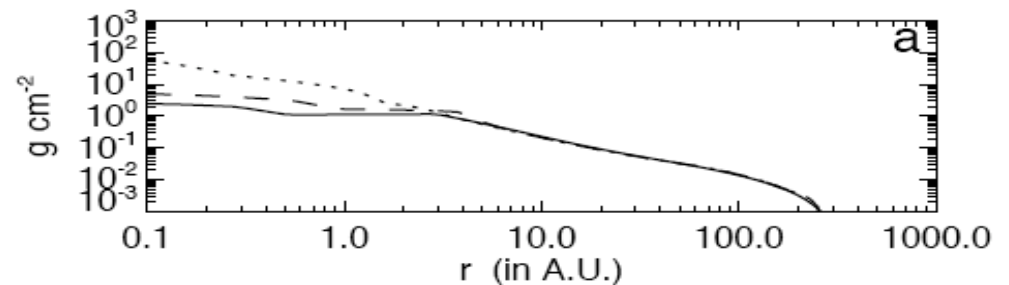
$$\text{suppose } \rho_{loc} \sim 0.1 \rho_{gas}; \text{ then } r \sim 1\text{m}$$



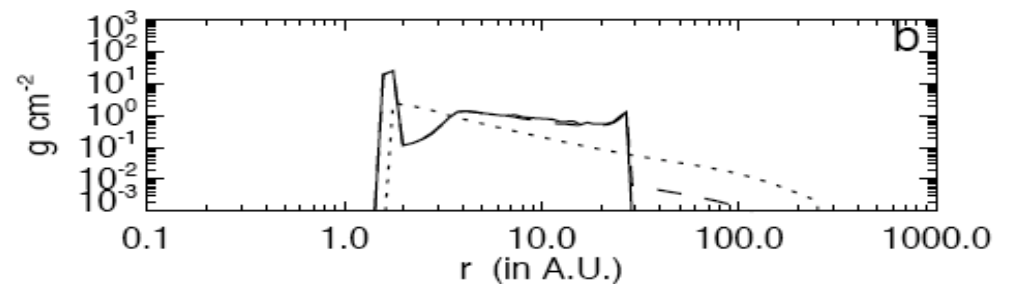
# Radial drift

Drift into the sun?

Significant mass transport  
may invalidate concept of  
“minimum mass nebula”



Stepinski and Valageas 1996, 1997





# Radial drift & evaporation fronts

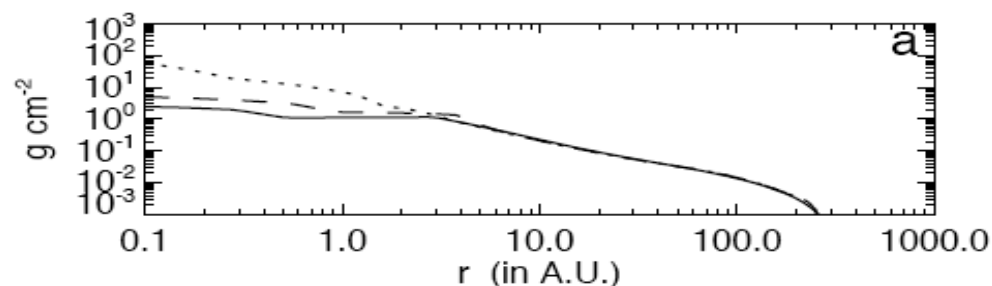
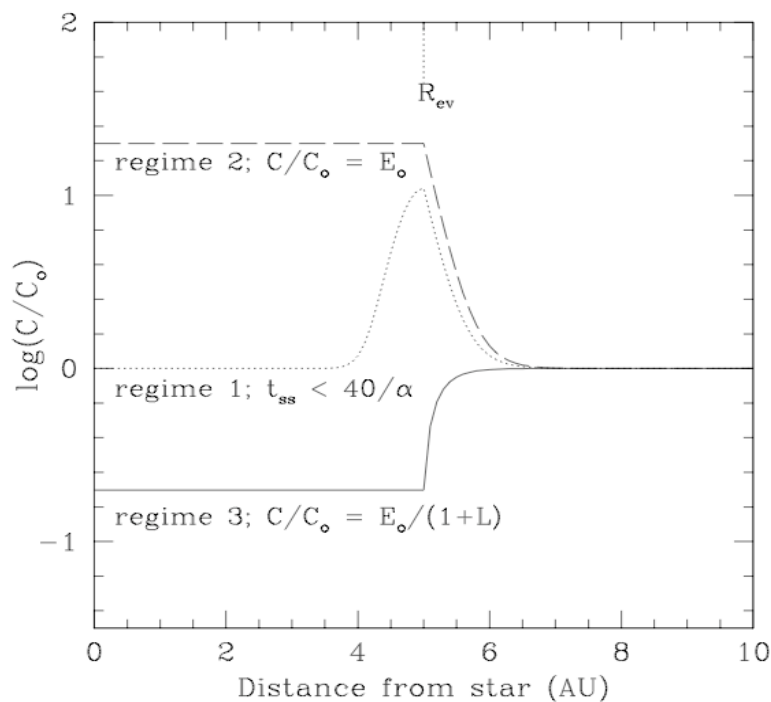
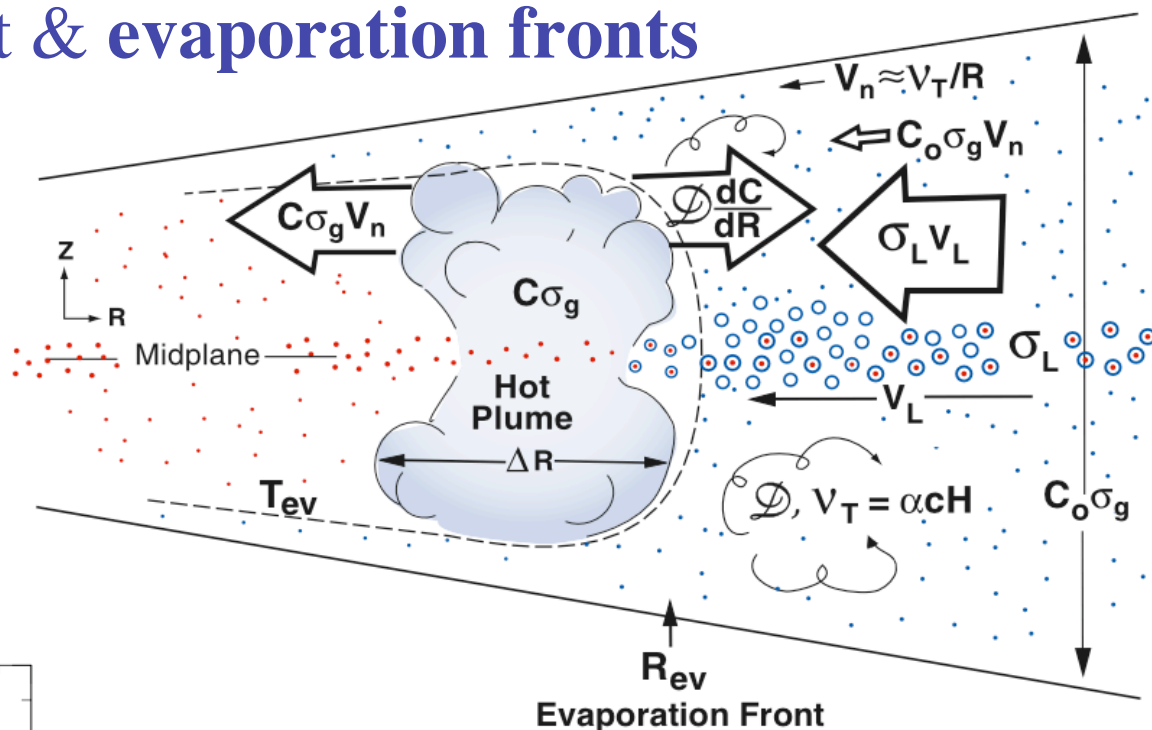
Drift into the sun?

Cyr et al 1998, Supulver & Lin 2000

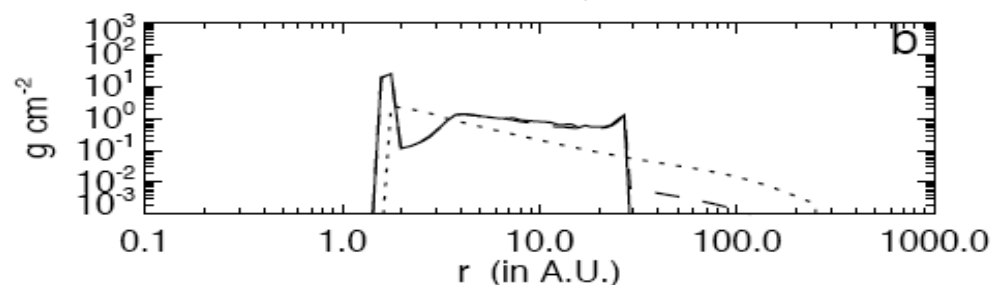
Cuzzi & Zahnle 2004 ApJ

Cuzzi et al 2003 Icarus

$$E \approx \frac{f_L V_L}{V_n} \approx \frac{f_L}{\alpha}$$



Stepinski and Valageas 1996, 1997





# Radial drift & evaporation fronts

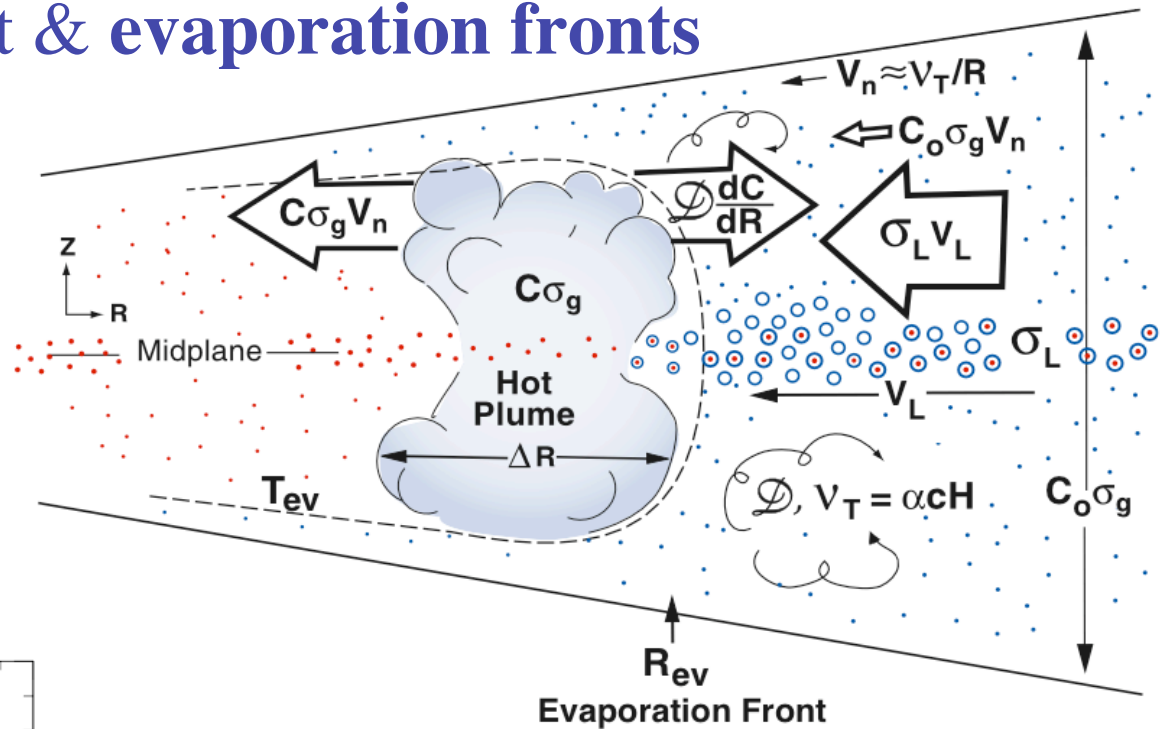
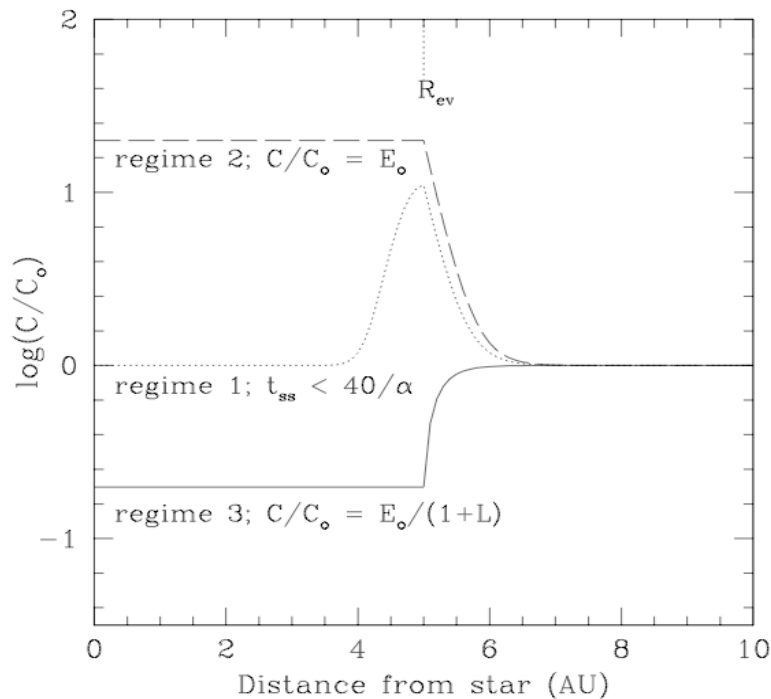
Drift into the sun?

Cyr et al 1998, Supulver & Lin 2000

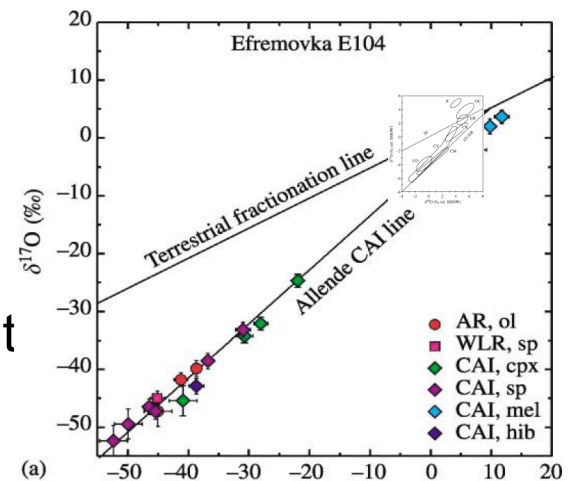
Cuzzi & Zahnle 2004 ApJ

Cuzzi et al 2003 Icarus

$$E \approx \frac{f_L V_L}{V_n} \approx \frac{f_L}{\alpha}$$



Water carries high  $^{17,18}\text{O}$  signal; radial transport leads to variable oxygen abundance and isotopic content





# Radial drift & evaporation fronts

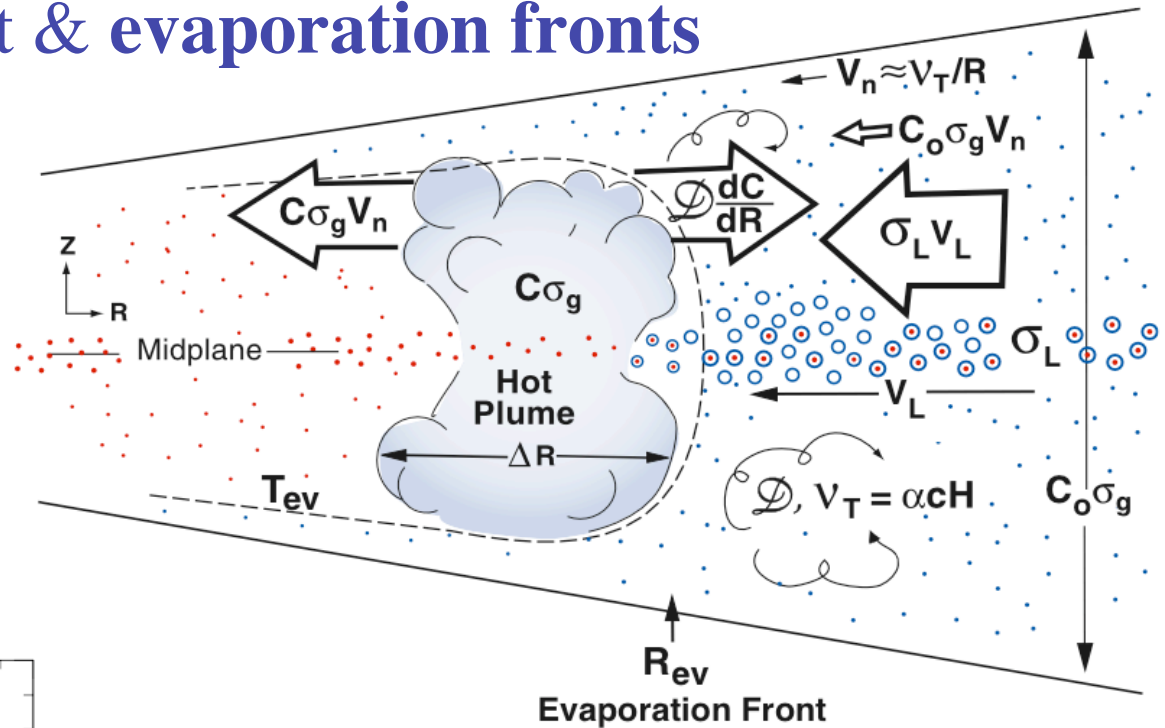
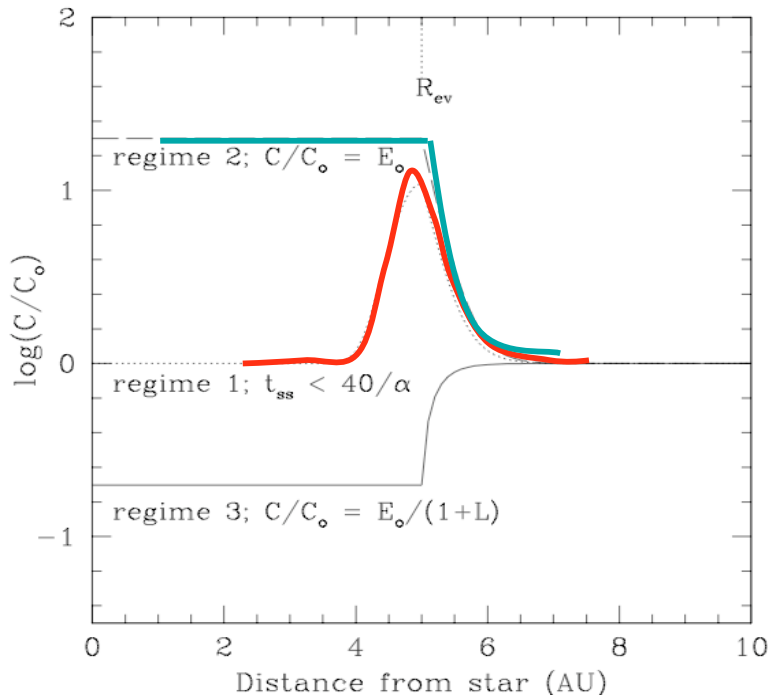
Drift into the sun?

Cyr et al 1998, Supulver & Lin 2000

Cuzzi & Zahnle 2004 ApJ

Cuzzi et al 2003 Icarus

$$E \approx \frac{f_L V_L}{V_n} \approx \frac{f_L}{\alpha}$$

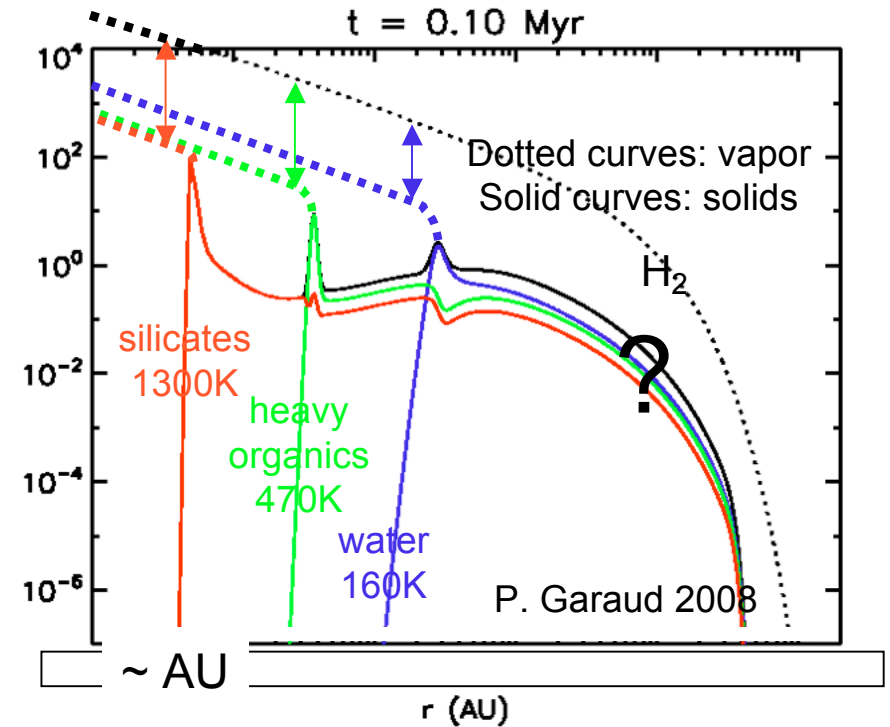
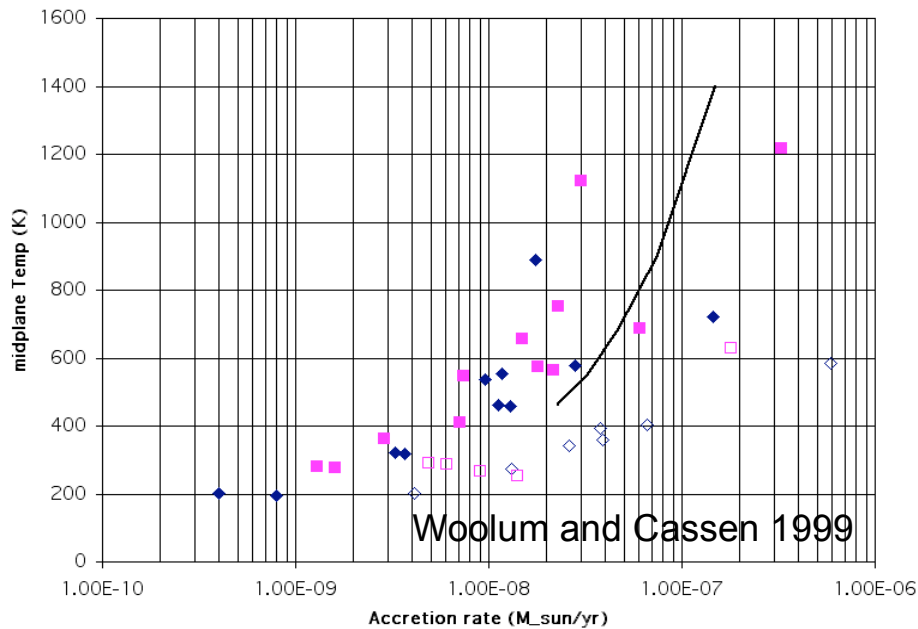


Future high resolution  
interferometric or spectroscopic  
studies might resolve EF structure;  
is it a **ring** or a **disk**?

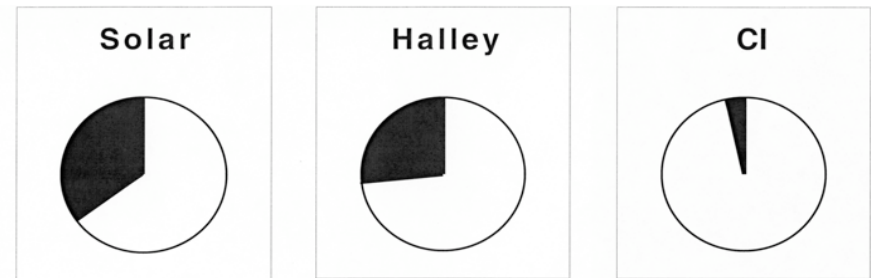
**Silicate/Carbon/etc EF's?**



# Early inner solar system: silicate EF?



Drifting primordial rubble  
is carbon-rich; refractory C/O  
in Halley is 40-50x chondritic



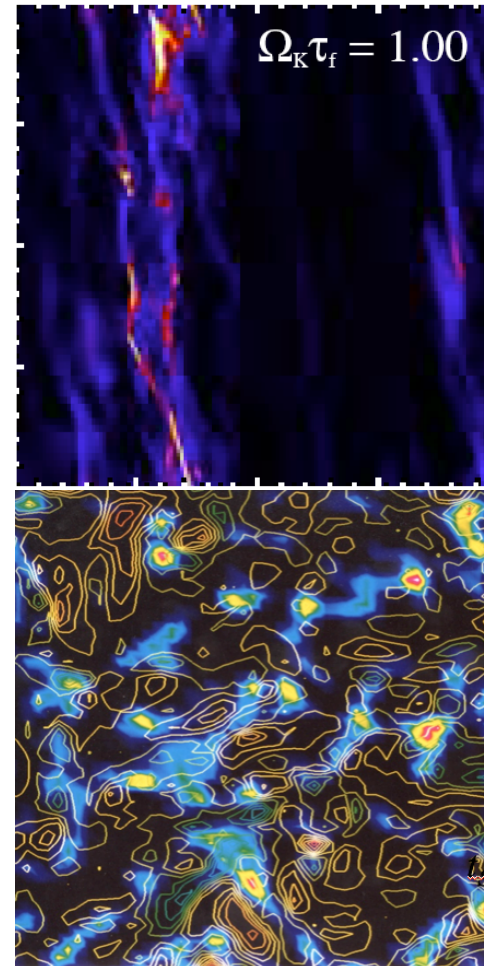
Production of  $\text{CO}/\text{CO}_2$  in *earliest*, hot inner nebula as evaporating silicates  
oxidize refractory carbon? Possibly decorrelated from  $\text{H}_2\text{O}$  abundance?  
(Najita et al, Carr et al, Eisner et al, Salyk et al, others)



## Presently two scenarios for planetesimal accretion in turbulence giving inefficient accretion :

Three-stage instability in *meter-size* particles triggered by pressure ridges around large-scale eddies, fostered by streaming instability, and completed by GI (Johansen et al 2007)

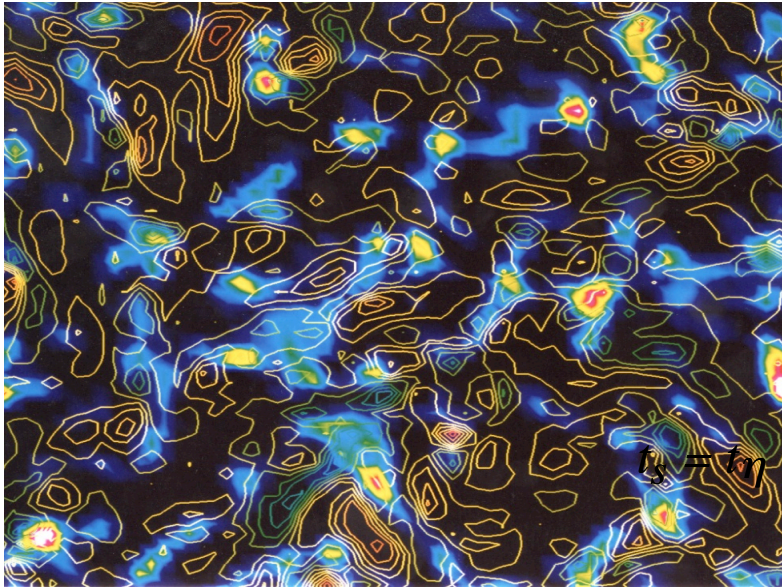
Two-stage instability in *mm-size* particles triggered by aerodynamic intermittency and completed by slow sedimentation under self-gravity (Cuzzi et al various)



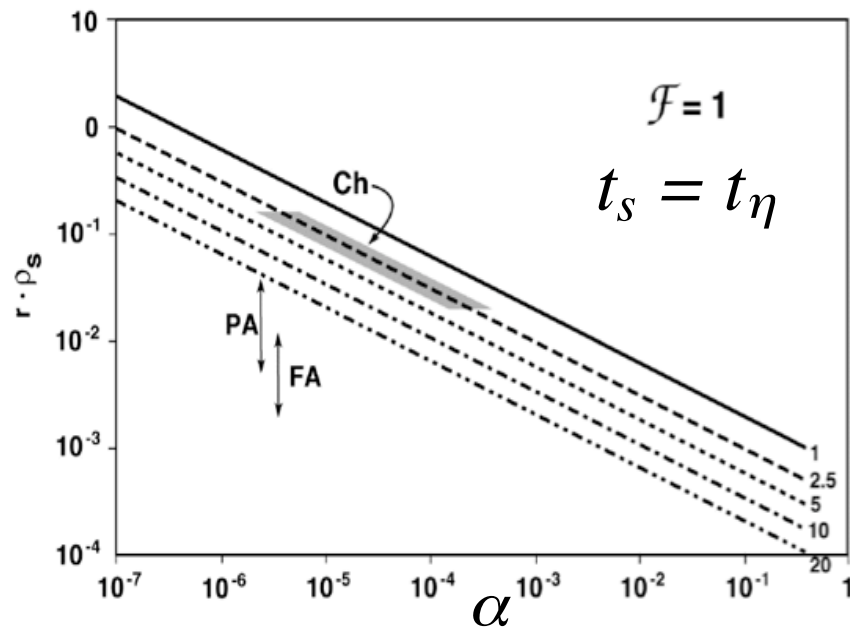
Both could operate independently in the same environment  
Both have issues to overcome



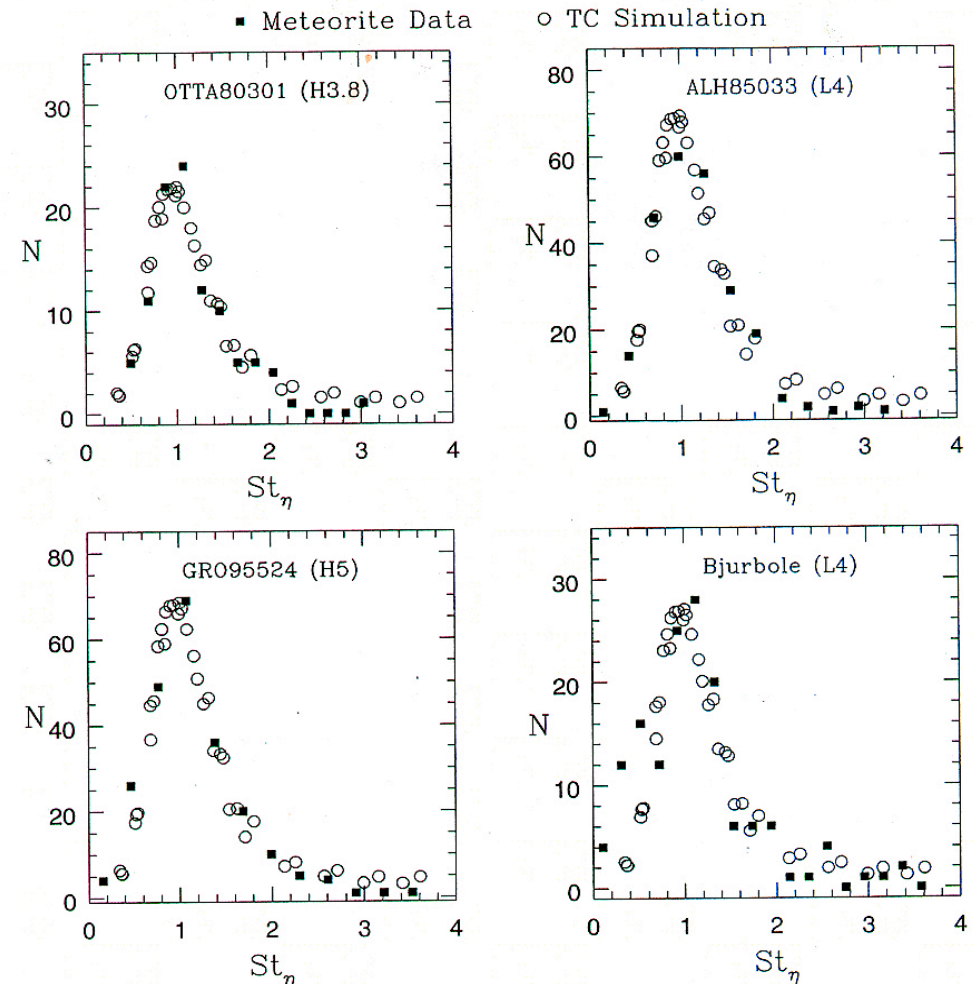
# Turbulent Concentration - “fingerprints”



Predicted size and size *distribution* are a good match to chondrules if  $St_\eta = 1$  at peak ( $t_s = t_\eta$ ) is assumed



Cuzzi et al 2001 ApJ



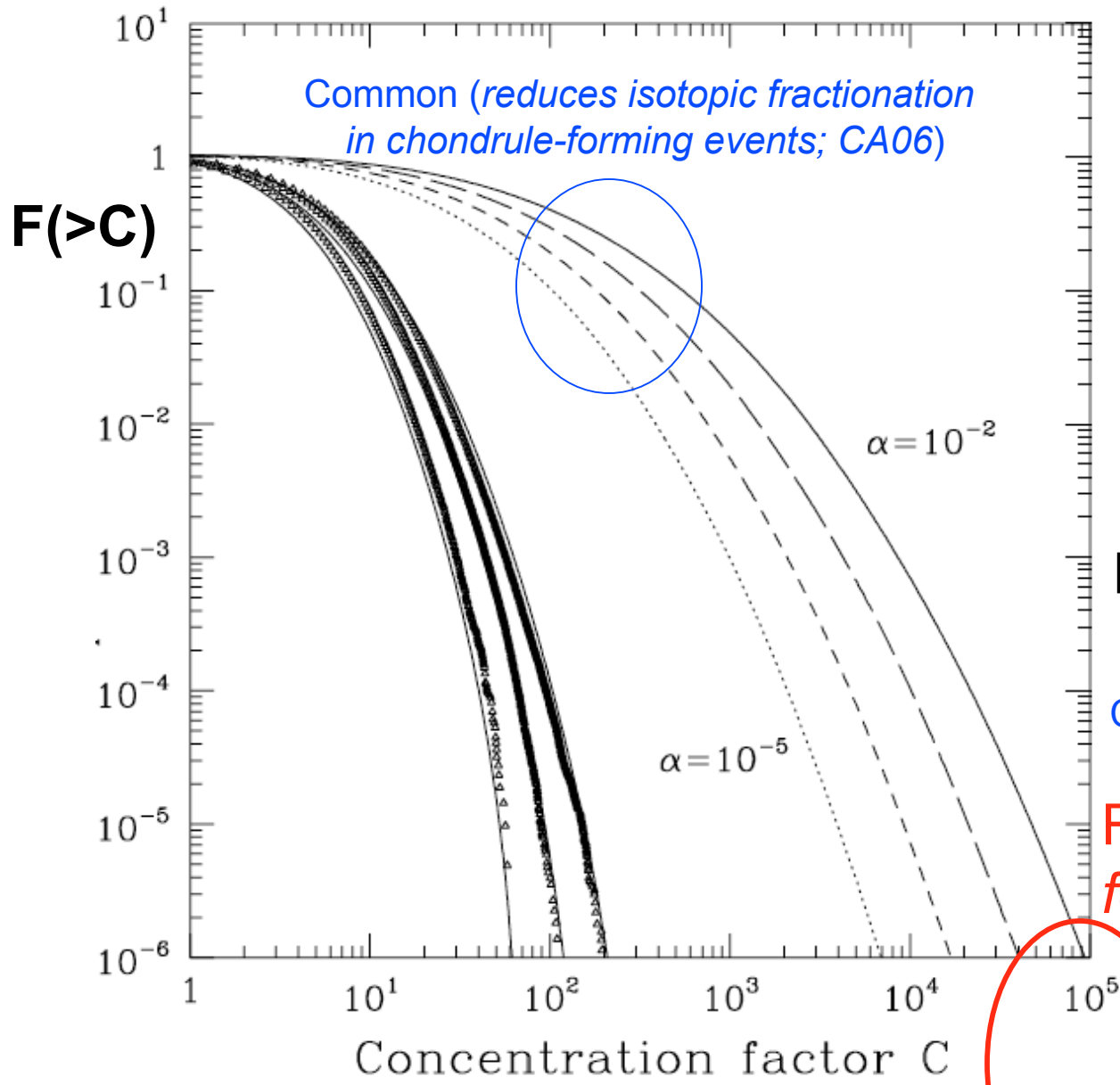




**Here was a movie.**



# Particle concentration factor (mass loading) follows a probability distribution $F(C)$



$F(C)$  depends on nebula turbulent intensity

$\alpha$ ;

Different mass loadings play different roles

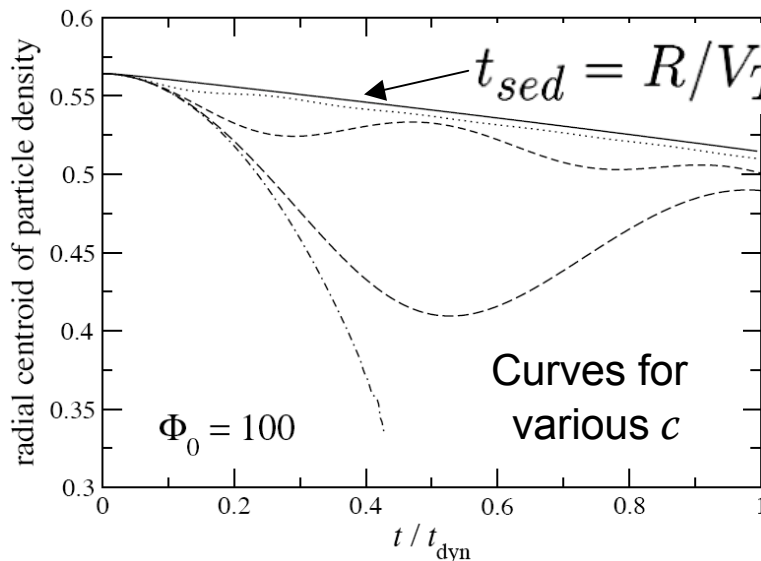
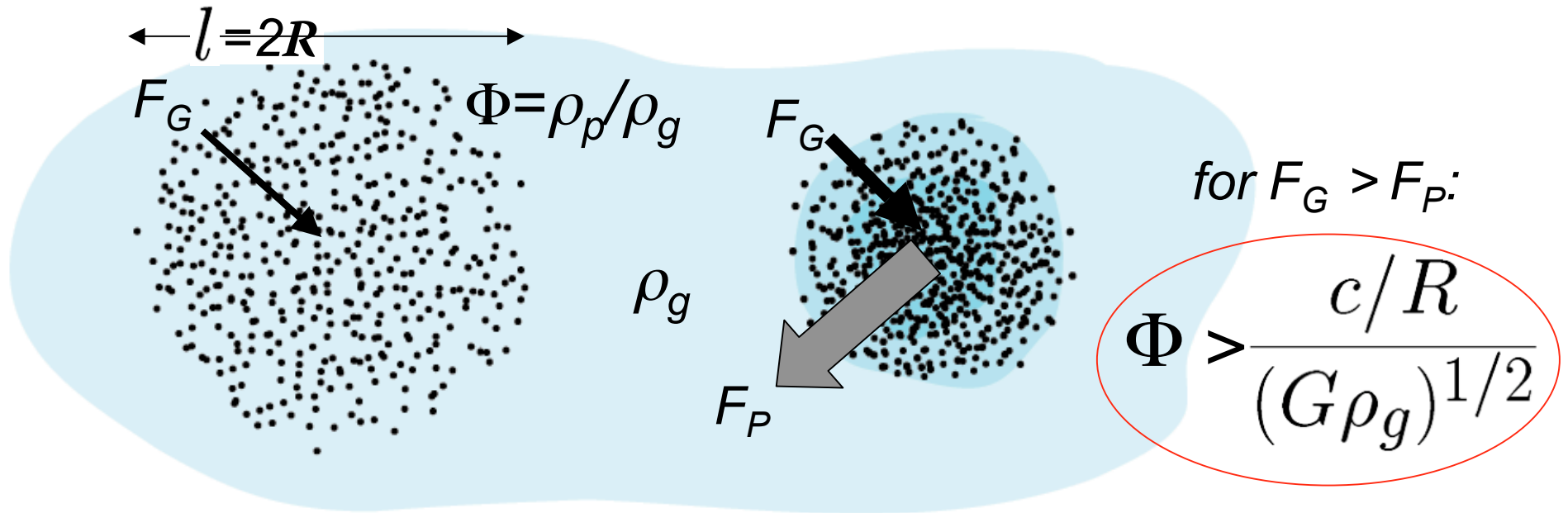
Cuzzi et al 2001 ApJ  
Cuzzi & Alexander 2006 Nature

Rare (dense enough for primary accretion)



# Gas pressure precludes GI for small particles!

(Sekiya 1983; but forgotten for 25 years)



Classical GI:  $\rho_p > 2\rho_R \sim M_\odot/2a^3 \sim \Omega^2/2G$

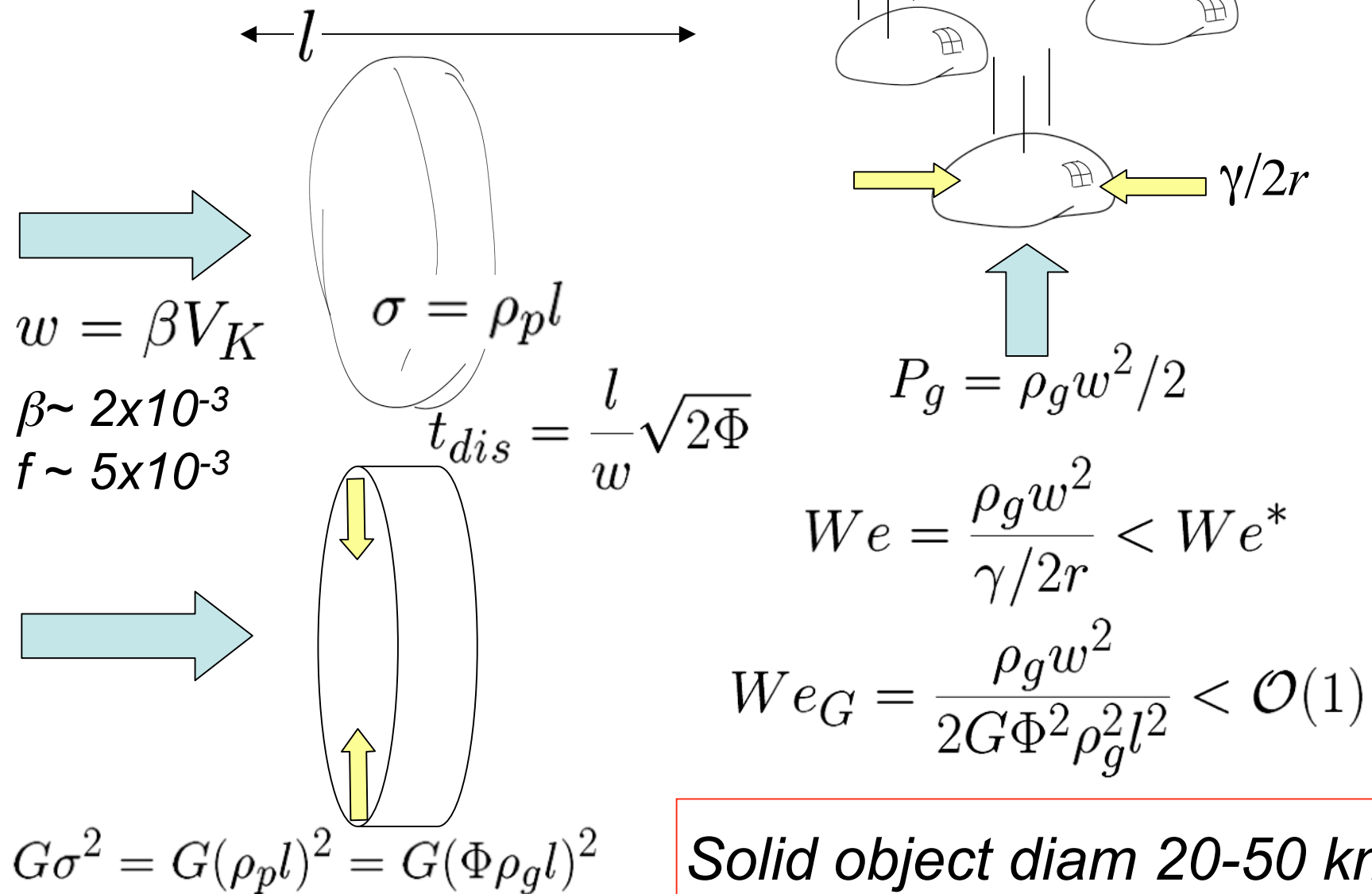
Safronov 1991, Goldreich & Ward 1973, Cuzzi et al 1993

$$\frac{\Phi}{\Phi_{\text{clas}}} = \frac{2c(G\rho_g)^{1/2}}{R\Omega^2} \sim 6000 \left( \frac{10^3 \text{ km}}{R} \right)$$

Sekiya 1983, Cuzzi & Weidenschilling 2006

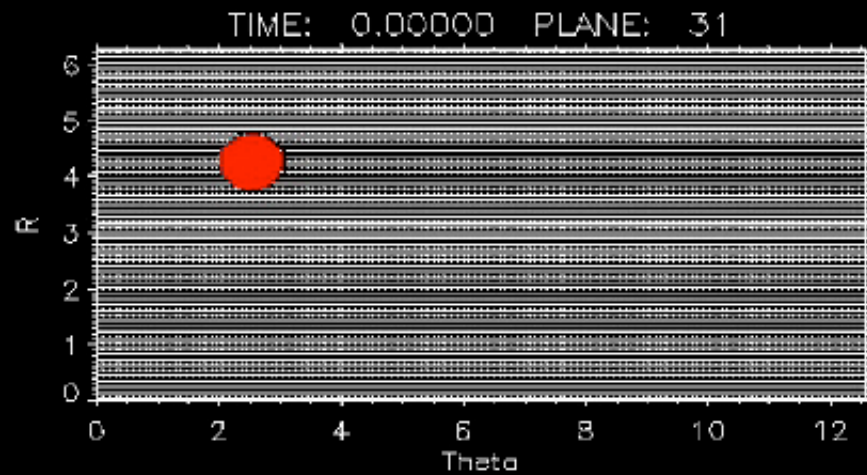
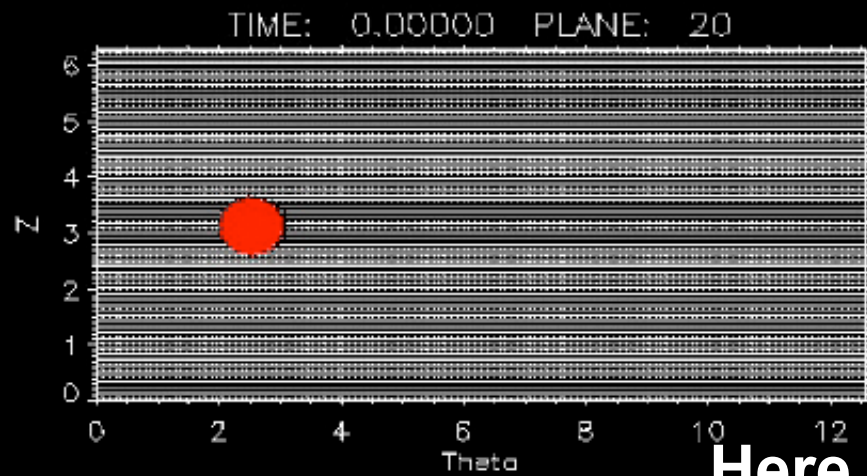


# Dense clumps destroyed by headwind ram pressure on the slow sedimentation timescale $t_{sed}$

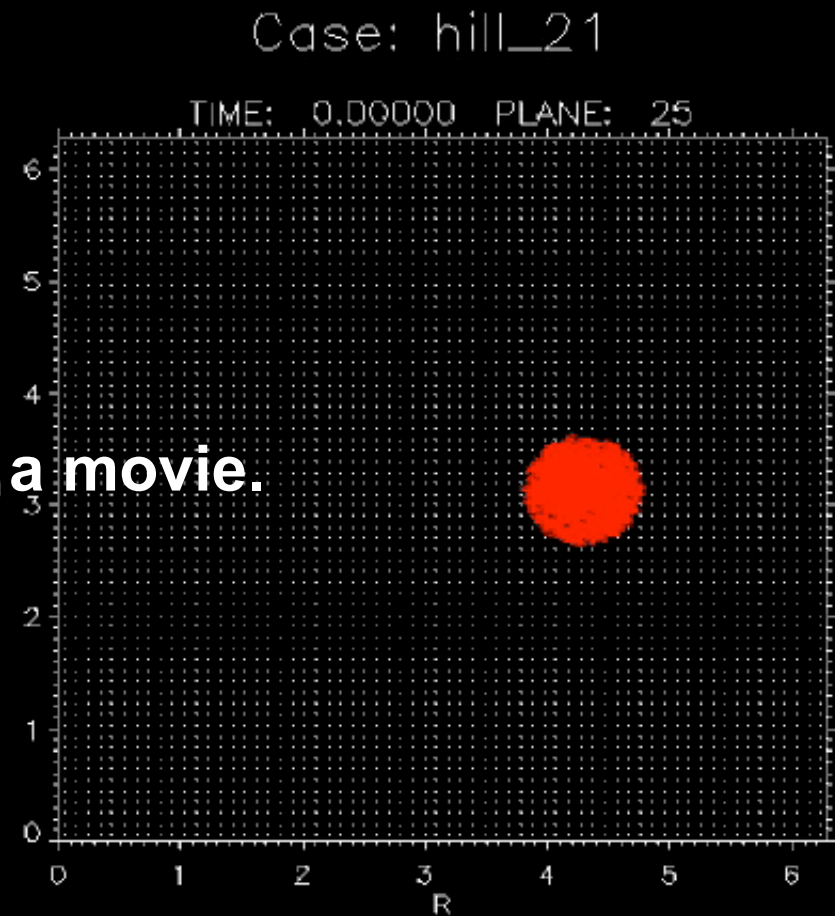




Simulation equivalent to  $\Phi=100$ ,  $l=10^4$  km,  $\beta=2\times 10^{-3}$   
*without* self-gravity

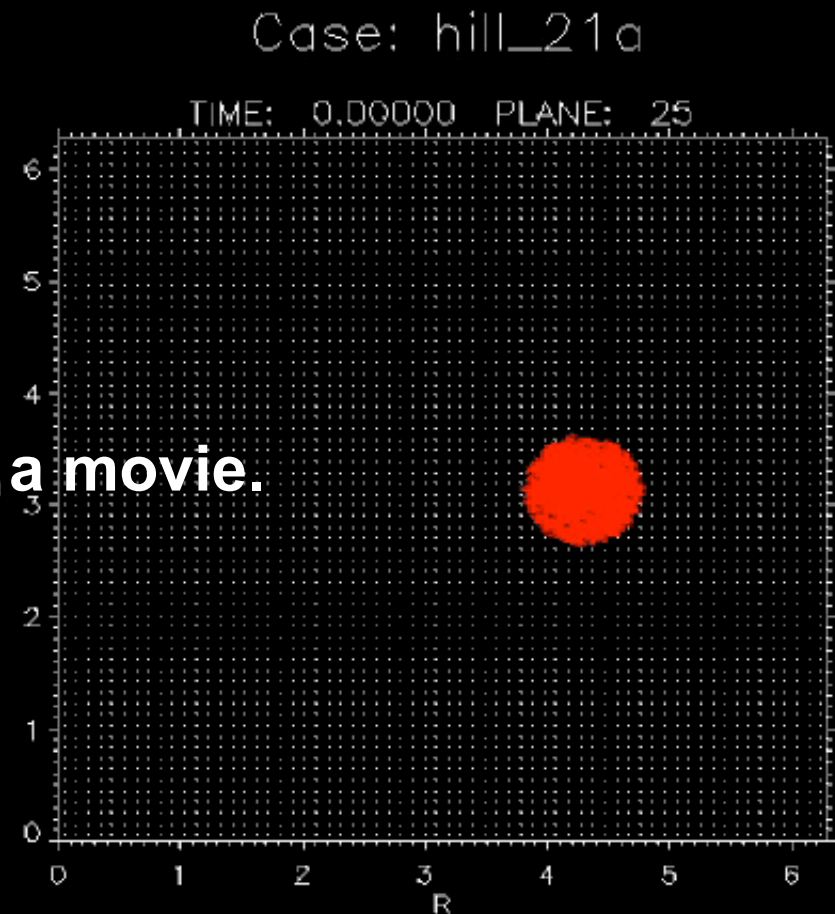
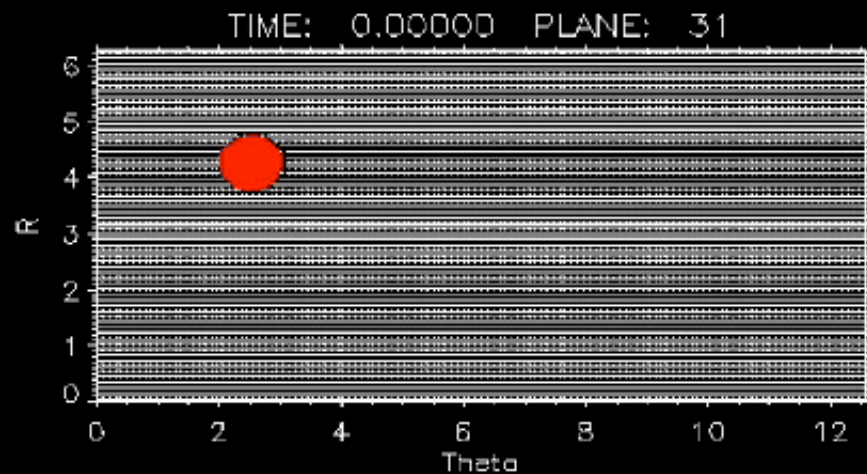
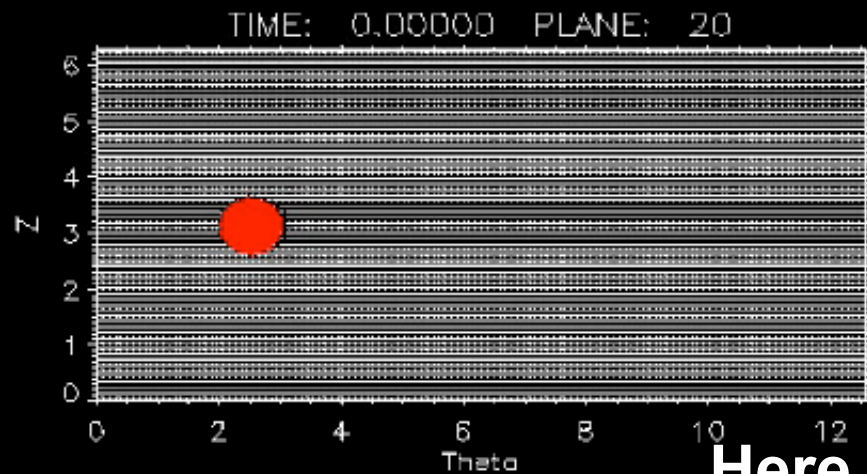


Here was a movie.



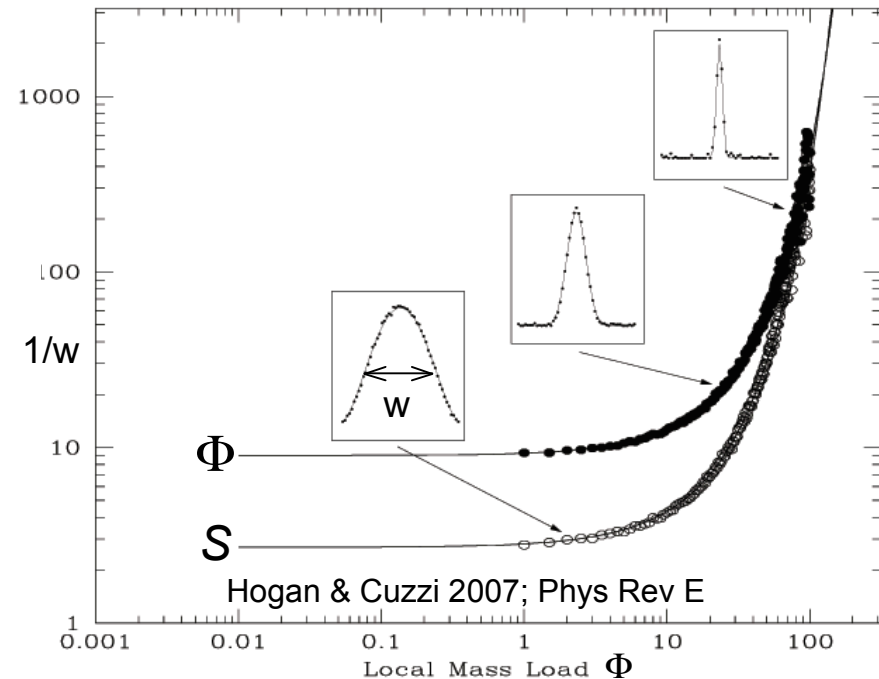
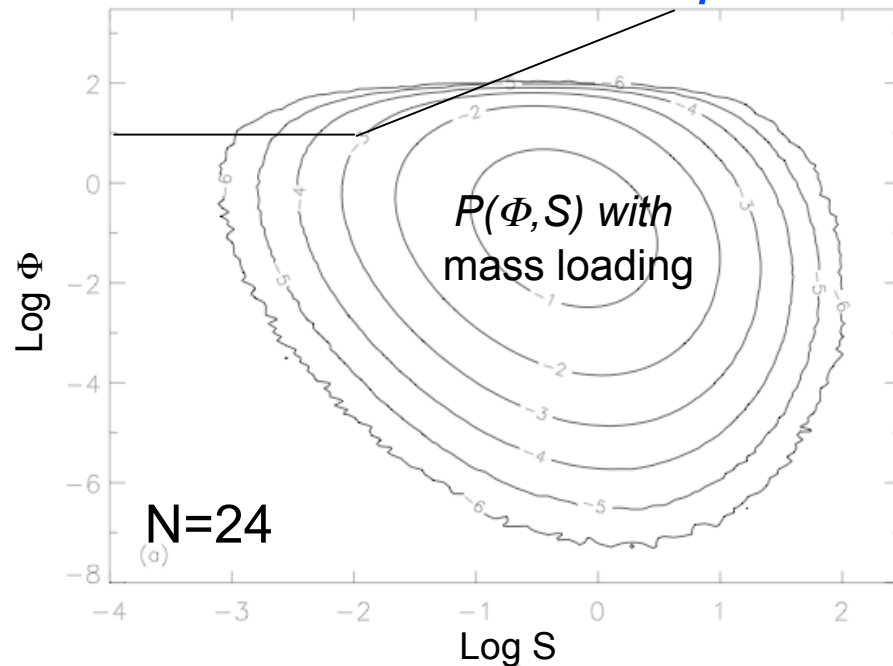


Simulation equivalent to  $\Phi=100$ ,  $l=10^4$  km,  $\beta=2\times 10^{-3}$   
*with* self-gravity;  $We_G$  criterion validated!





# Determining the **creation rate** of suitable clumps at $(\Phi, l)$ : *Cascade model of **particle-laden** turbulent concentration*



Use multipliers to determine  $P(\Phi, S)$  = Joint PDF of  $\Phi$  and vorticity  $S$

- includes known spatial anticorrelation of the two quantities.
- checked against exact 3D turbulence simulations; good agreement
- can be run to **far** higher  $Re$  than CFD simulations (*ie*, to nebula  $\alpha$ )

Mass loading saturates  $P(\Phi, S)$  at  $\Phi \sim 100$

$P(\Phi, S)$  then used to calculate  
*formation rate and mass of primary planetesimals*



# Summary of this primary accretion scenario

Nebula particulate mix may be slowly varying radially  
but evolves with time (chemistry, isotopes, mass)

Local abundances of solids & vapor can be greatly enhanced  
by rapid radial drift of “boulders” from further out

Chondrules are formed by heating in common dense clumps  
which have concentration  $\sim$  hundreds of times “cosmic”

Rare, very dense clumps become gravitationally bound  
and sediment inwards to form 10-100km “sandpiles”

Sandpiles contain well-characterized, size-sorted particles  
of size which depends on local gas density and  $\alpha$

Process can operate anywhere but “fingerprints” may be  
less apparent where only fluffy aggregates exist

Statistical techniques are needed to assess whether  
primary accretion “rate” satisfies constraints



# Open issues and good areas for future work

Turbulence: MRI vs hydrodynamical production?  
sporadic and/or layered turbulence?  
can turbulence be measured observationally?

Lab experiments on strength/compressibility of aggregates  
(size distributions, tensile/compressive; etc)

Coupled growth / drift / radiative transfer / thermal modeling  
possible applications to inner and outer nebula problems

Interferometric/spectroscopic observations of early disks  
evidence for unusual vapor abundances inside EFs?

Primary accretion: behavior of dense clumps in turbulence  
(collision? disruption/coagulation? statistics?)